



## Analysis, Design, Optimization and Realization of Compact High Performance Printed RF Filters

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# <span id="page-2-0"></span>**Dedications**

 $This work is \ dedicated to \ my \ Father \ and \ to \ the \ memory \ of \ my \ Mother$ 

 $Atallah$ 

## <span id="page-4-0"></span>Acknowledgement

First of all, I would like to thank God, who gives us every thing and without him nothing can be done.

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# <span id="page-6-0"></span>Kurzfassung

In der vorliegenden Arbeit wird ein modifizierter Querschnitt der mehrschichtigen Koplanarleitung und seine Anwendung fuer Filterzwecke untersucht. Mit Hilfe dieses Querschnittes wurde ein Tiefpass entworfen, der durch das Anbringen von breiten Patches auf dem klassischen Koplanar Waveguide (CPW) Tiefpassfilter realisiert wird. Die Patches sind auf der Ruckseite des Substrates und unter dem kapazitiven Streifen angebracht. Weitere Filter mit Bandpasscharakteristik sind so aufgebaut, dass sie Mikrostreifenleitung, CPW oder aus beiden beinhalten. Ein in der Mitte des Hohlleiters angebrachtes Streifenleitungs-Ultrabreitband-Bandpassfilter mit einem breiten Sperrbereich basiert auf einem Tiefpassfilter, das mit Ein/Aus- Versorgungsleitungen kapazitiv gekoppelt wird.

In dieser Arbeit wird auch ein interdigitaler Defected Ground Schlitz vorgestellt und untersucht. Zwei Tiefpassfilter werden dargestellt, die diesen Schlitz benutzen und dabei die Vorteile von kompakten Slots aufzeigen. Es wird eine Losung gezeigt, die die Schwierigkeiten beim Aufbau von Gehausen reduziert, indem die Grundplatte der Schaltung voll metallisiert wird und Schlitze auf dem Substrat geatzt werden. Das Metall des Substrates ist mit der Grundplatte mit Hilfe von Durchganglochern verbunden.

Es konnte ein erster Mikrostreifen-Resonators realisiert werden, der drei Resonanzfrequenzen besitzt. Dieser Resonator ist so aufgebaut, dass eine zusatzliche Maander-Mikrostreifenleitung von halber Wellenlange hinzugefugt wurde, die an den zwei gegenuberliegenden Ecken des originalen quadratischen Mikrostreifen- Zweimodenresonators verbunden ist. Zwei Bandpassfilter wurden realisiert mit Hilfe dieses Resonators, der erste mit einer Nullstelle in seinem Sperrbereich und der zweite mit drei Nullstellen. Weiterhin wird auf der Basis von Streifenleitungen ein Hohlleiter-Zweimodenresonator vorgestellt, es ist der erste Zweimodenresonator in dieser Technologie.

Zwei weitere kompakte Filter werden entworfen, gefertigt und getestet, die zwei Durchlassbereiche besitzen und auf dem Einsatz eines Zweimodenresonators aufbauen. Der erster Filter ist ein Mikrostreifen- Filter, er wurde realisiert durch das Einfugen von Nullstellen im Durchlassband eines Breitbandfilters durch die Benutzung eines quadratische scheifen Zweimodenresonator. Der zweite Filter ist ein Filter mit

bereits vorher vorgestellten Hohlleiter-Streifenleitungen. Der Filter wurde realisiert durch die Aufteilung der Moden von Zweimodenresonator in zwei Frequenzbander.

## <span id="page-8-0"></span>Abstract

This thesis introduces and investigates different multilayer structures and their filter apllictions. Compact quasi-lumped filters are introduced using this technology. Low-pass filter is designed using this structure by adding wide patches to the classical coplanar waveguide low-pass filter at the back side of the substrate and under the capacitive lines. Bandpass filters are introduced, these filters are constructed to be integrated with microstrip line, coplanar waveguide, and both. Moreover, a suspended stripline ultra-wideband bandpass filter with very wide stopband is introduced by coupling low-pass filter capacitively with the I/O feeding lines. The thesis also introduces and investigates an interdigital defected ground slot. The slot is very compact compared to the other known slots. Two low-pass filters are presented using this slot showing advantages of the compact slot. Moreover, the thesis presents a solution to reduce the packaging difficulties by keeping the ground plane of the circuit fully metallized and etching the slots on the superstrate, which is directly laying on the top of the substrate. The metal of the superstrate is connected by via holes to the ground plane. Further more, the thesis also introduces the first microstrip realization of triple-mode resonator. This resonator was realized by adding an additional meander half wavelength microstrip line connected to two opposite corners of the original microstrip square-loop dual-mode resonator. Two bandpass filters are realized using this resonator, the first one with a transmission zero in its stopband, and the second one with three transmission zeroes in its stopband. Moreover, a realization of suspended stripline dual-mode resonator is presented in this thesis, which is the first dual-mode resonator for this technique. Very compact bandpass filters are designed fabricated and tested using this resonator. Dual-band bandpass filters are realized by using dual-mode resonators. The first filter is a microstrip one is realized by introducing transmission zero in the passband of a broadband bandpass filter by using square-loop dual-mode resonator. The second introduced filter is a suspended stripline one. The filter is realized by splitting the modes of the dual-mode resonator into two frequency bands.

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# <span id="page-20-0"></span>Chapter 1 Introduction

The increasing scale of modern wireless communication applications and radar systems in today's technology has boosted the demand for RF and microwave filters; as they are playing an essential role in Transmit-Receive systems. Such as radio and television broadcasting, mobile communications, satellite communications, traffic radar, air traffic radar, automotive radar, and synthetic aperture radar. Fig. 1.1 shows a simple scheme of the radio system, while Fig. 1.2 shows a simple scheme of the doppler radar.



Figure 1.1: Simplified schematic of a basic radio transmitter (up) and receiver (down).



Figure 1.2: Simplified schematic of a doppler radar.

The microwave and RF filters are two-port frequency selective networks [\[1,](#page-134-0) [2,](#page-134-0) [5\]](#page-134-0). The main application of the filter is to reject the unwanted signal frequencies while permitting a good transmission for the required frequencies. These networks are classified according to their application. There are four main filter classes . The first class is lowpass filters which provide good transmission for low frequencies and reject the high frequencies, this kind of filters are used to suppress harmonics and spurious, which is necessary in designing power amplifiers, mixers, and voltage-controlled oscillators [\[1\]](#page-134-0). The second one is highpass filter which rejects the low frequency and provides a good transmission for high frequency, this filter has many applications such as removing the DC offsets and removal of low-frequency noise. The third one is bandpass filter that provides good transmission for a certain frequency band and rejects the lower and upper frequency bands, this kind of filters is used in many applications to select certain frequency band. The forth and last common filters is bandstop filter which provides rejection at certain frequency band and provides good transmission at lower and upper frequency bands [\[1\]](#page-134-0), [\[2\]](#page-134-0) and [\[5\]](#page-134-0).

Another application for filters is to separate between different frequency bands as it is in the case of diplexers and multiplexers. which are multiple port components. These components are realized by connecting two or more filters - each operates on different frequency band - in parallel or in series, see e.g. [\[1\]](#page-134-0), [\[6\]](#page-134-0). By using the diplexers and multiplexers as multiple output and single input. It can also be used for different application, which is summing the signals that have different frequency bands, by using it as multiple input single output device .

RF and microwave filters are also classified by technology used for the filter realization into active and passive filters. Active filters are realized by using active elements such as transistors, diodes and amplifiers, in addition to the passive components. These filters are simple to realize, they provide gain, high quality factor, and can be easily integrated with the other system components. However, due to the active elements used in the filter, the filter requires a power supply, which may increase the complexity to the system. Moreover, the internal feedback is required, that may increase the sensitivity of the filter [\[7\]](#page-134-0).

Passive filters are realized by using passive elements such as capacitors and inductors. This kind of filters has many advantages over active filters, they are more stable than the active filters, no power supply is required, and less expensive.

For microwave range higher than 500 MHz, the passive filters are mostly realized by using either planar transmission lines, or waveguides. Although waveguide components have low losses, and can handle higher power than the planar transmission lines, it is not preferable in new communications systems that require the mobility, because of their large size and their heavy weight. Moreover, fabrication processes of the waveguide components are more expensive than that for planar transmission lines. Therefore, most of microwave filters are designed using the planar transmission lines.

### <span id="page-22-0"></span>1.1 Planar Resonators

Modern systems require high performance filters with very low losses, small size, sharp cut-off, and high rejection at the stopband. Thus, different resonators and techniques have been introduced for RF and microwave filters to achieve different filters with this performance using the planar transmission line. The main used resonators and techniques are:

- 1. Folded Transmission Line Resonator: It is the simplest resonator, it is basically a transmission line section that resonates when its length corresponds to half a wavelength  $|1|$ .
- 2. Stepped Impedance Resonators: This type of resonators consists of high and low impedance sections, or in other words wide and narrow width transmission lines. This resonator resonates when its length corresponds to half a wavelength [\[1\]](#page-134-0), [\[2\]](#page-134-0),and [\[5\]](#page-134-0).
- 3. Open-Loop Resonators: It is a modified version of folded transmission line resonator, it is also known as U-shaped resonator and hairpin resonator, it looks like a loop which open from one side, see Fig. 1.3. This type of resonators has great advantages in reducing filter size, in addition, it has different coupling nature depending on the coupling sides [\[2\]](#page-134-0), [\[4\]](#page-134-0), and [\[8\]](#page-134-0). The main disadvantage of these resonators is that the higher order harmonic does not allow for wide stopband.



Figure 1.3: Two possible shapes of open-loop resonator.

4. Dual-Mode Resonators: This type of resonators is considered to be one of the most compact resonators used for the filter design these days. This is because, e.g., a second order filter can be realized by using a single resonator, in turn the size of the filter can be reduced to the half of that in case of single resonance resonators, such as half-wavelength folded line resonator. In addition, quasi-elliptic filter responses are easily achieved using such resonators without main change on the filter structure [\[9\]](#page-134-0), [\[10\]](#page-134-0) and [\[11\]](#page-135-0). The traditional dual-mode <span id="page-23-0"></span>resonators are realized by using a square or circular desks or loops, these resonators are normally fed by perpendicular feeding lines, see Fig.1.4. Fig. 1.5 resemble two minima that corresponds to the resonance of the structure.



Figure 1.4: Dual-mode resonator fed by perpendicular feeding lines .



Figure 1.5: Return loss of dual-mode bandpass filter using one dual-mode resonator.

5. Multiple-Mode Resonators: This type of resonators has multiple resonance behavior in its passband. Many resonators of this type have been introduced. In [\[12\]](#page-135-0) a multiple-mode resonator was introduced by using half-wavelength transmission line connected with pair of open end stubs, the resonator has been modified in [\[13\]](#page-135-0) by replacing the open-stubs by shunted stubs. A multiplemode resonator has been introduced by using pair of coupled rings with two open stubs symmetrically tapped to the inner ring [\[14\]](#page-135-0). A simple resonator of <span id="page-24-0"></span>this type was realized by stepped-impedance transmission line with length of  $\lambda$ at the center frequency in [\[15\]](#page-135-0).

- 6. Defected Ground Resonators: It is a technique that has been recently introduced for mirostrip and complanar waveguide. It simply introduces resonances by etching slots in the ground plane of the mirostrip and complanar waveguide. different slot shapes have been introduced for filter applications, such as square head dumb-bell [\[16\]](#page-135-0), rounded head dumb-bell [\[17\]](#page-135-0), U-shape slots [\[18\]](#page-135-0), and many other slot shapes [\[19](#page-135-0)[–23\]](#page-136-0). The main advantages of this technique are reducing the size of the filter, increasing the degree of freedom since the resonator can be built on ground plane. However, this technique enlarges the packaging efforts.
- 7. Quasi-Lumped Resonators: Quasi-lumped elements and resonators have been introduced some years ago by using very small transmission line section [\[24–](#page-136-0) [27\]](#page-136-0). Since the filter is realized by short line sections, the over all filter structure becomes small, and therefore the filters designed using quasi-lumped elements have low losses and wide stopband. Different filters with different bandwidths were introduced using the quasi-lumped elements technique [\[25–27\]](#page-136-0).

## 1.2 Planar Lowpass Filters

Stepped impedance transmission lines have been first known structure for lowpass filter design [\[1,](#page-134-0) [2,](#page-134-0) [5\]](#page-134-0). Lowpass filters are normally realized by cascading high and low-impedance transmission lines. each of these lines must have very short length. The number of the used line section represents the order of the filter [\[28\]](#page-136-0). Fig. 1.6 shows a seventh order stepped impedance microstrip lowpass filter. The rejection at the stopband of such filters is not sufficient, and since most of the filter applications require filters with sharper cut-off, many techniques have been introduced in order to increase the rejection of the filter at the stopband.



Figure 1.6: Top layout of stepped impedance microstrip lowpass filter.

According to the basics of the filter, sharper cut-off slop and better rejection can be obtained by increasing the order of the filter. However, the higher the filter order, the higher the losses. Another way to increase the cut-off sharpness is introducing <span id="page-25-0"></span>transmission zeros at the stopband of the filter response, which can be done by two approaches. The first approach is realized by introducing series resonator instead of shunt capacitance. This approach can be achieved using the planar technology by different ways. First one is done by implementing open-circuited quarter-wavelength stubs instead of the low-impedance transmission line sections, e.g. [\[1,](#page-134-0) [2,](#page-134-0) [5\]](#page-134-0), see Fig. [2.17a](#page-47-0). The open stub act as a short circuit when its length corresponds to quarter a wavelength, so a transmission zero can be introduced at that frequency. To reduce the length of the stubs, stepped-impendence stubs have been introduced [\[29\]](#page-136-0), [\[30\]](#page-136-0), see Fig. [2.17b](#page-47-0).



Figure 1.7: Low-pass filter structure (a) with quarter-wavelength stub, (b) with stepped-impedance stub.

The second approach is realized by introducing parallel resonators instead of series inductance. In the planar techniques, this has been realized by increasing the coupling between the low-impedance transmission line sections, by either extending the lowimpedance line sections in parallel to the high-impedance line section [\[31,](#page-136-0) [32\]](#page-136-0), as shown in Fig. [1.8,](#page-26-0) or by using snaked high impedance transmission line [\[33\]](#page-137-0).

Transmission zeros can be easily introduced to the filter response without main change on the filter structure, by using defected ground structure technique (DGS). For lowpass filter, slots are mostly etched under the high impedance transmission lines, to introduce series capacitance in parallel to the inductive transmission line,

<span id="page-26-0"></span>

Figure 1.8: Low-pass filter structure with extending the low-impedance line sections in parallel to the high-impedance section .

which in turn introduces transmission zero. Normally the number of transmission zeros introduced for the lowpass response is equal to the number of the slots etched in ground plane, see [\[16\]](#page-135-0), [\[17\]](#page-135-0), [\[23\]](#page-136-0), and [\[34–37\]](#page-137-0).

### 1.3 Planar Bandpass Filters

Bandpass filters is one of the most important filters in the communication systems, they are classified by their bandwidth to narrowband, wideband and ultra-wideband filters. The main challenges that face the filter designers are to design a bandpass filter with compact size, low losses, and wide stopband.

#### 1.3.1 Narrowband and Wideband Bandpass Filters

The early efforts were introducing end-coupled transmission line resonators [\[38\]](#page-137-0). It basically consists of transmission line sections having a length of half-wavelength at the corresponding center frequency. These transmission lines are coupled to each other by a small gap, as shown in Fig 1.9. The gap between the resonators is introducing a capacitive coupling between the resonators, which can be represented by a series capacitance [\[2\]](#page-134-0).





Side coupled half-wavelength transmission lines filter is a another bandpass filter structure [\[39\]](#page-137-0). The resonators are sidely coupled along of their length, as shown in <span id="page-27-0"></span>Fig. 1.10. Using this configuration, higher coupling is obtained and therefore wider bandwidth can be achieved.



Figure 1.10: Layout of microstrip bandpass filter using half-wavelength side coupled resonators.

Many other filters and resonators have been introduced and designed, such as stub type resonators. Filters of this type are designed using this resonator by either shunt open-circuited half-wavelength stubs or shunt short-circuited quarter-wavelength stubs [\[1,](#page-134-0) [2,](#page-134-0) [5\]](#page-134-0). A more compact bandpass filter is combline and quasicombline filters. these filters are realized be having array of coupled resonators. The input and output are connected to the first and last array element which are not considered to be resonators [\[2\]](#page-134-0). Another resonator is hairpin-resonator that is also known as U-shape resonator,or open-loop resonator. It resonate at half-wavelength of the corresponding frequency. This resonator is more compact than the previous two resonators. Many other compact filters and resonators have been introduced in the past. In the next chapters we will discuss some other resonator types that have small size and high performance.

Wideband bandpass filters with fractional bandwidth greater than 25% are mostly realized by increasing the coupling between the resonators. To increase the coupling for the end-coupled resonators, multilayer structure has been used [\[40\]](#page-137-0). For the sidecoupled resonator filters, apertures have been opened under the coupling area [\[41\]](#page-137-0).

#### 1.3.2 Ultra-Wideband Bandpass Filters

Ultra-wideband systems are defined as those systems that operate with fractional bandwidth greater than 40%. These systems have main advantages in transmitting high data rate with low power. In the recent years, ultra-wideband communication system specification has been defined for indoor applications, this system operates on 3.1-10.6 GHz [\[42\]](#page-137-0). For such systems, bandpass filters with fractional bandwidth of 110% is needed. The available filter theory however is not valid for this specification. Furthermore, the available resonators have not succeeded in providing such bandwidth. Therefore new resonator structures have been proposed, which is multiplemode resonator [\[15\]](#page-135-0). In order to let the resonator give such wide passband, the coupling strength between the resonator and the feeding line has been increased by using locating the feeding lines and the resonator on the opposite sides of the substrate [\[43\]](#page-137-0). The main challenge for this class of resonators is to have wide stopband,

<span id="page-28-0"></span>therefore different modifications have been done on this resonator, such as using defected ground structure under the resonator [\[44\]](#page-137-0), the most successful one is done by using stepped impedance [\[45\]](#page-138-0). However, with these modifications some of these filters are suffering from bad matching the passband, some others suffer from high group delay variations in the passband.

#### 1.3.3 Dual-Band Bandpass Filters

Some of the modern multi functional communication systems work with signals spread at the same time with several frequency bands, therefor these systems must incorporate dual-band, triple-band or multi-band filters. Thus, different efforts have been made on designing filters with this specification. The most known dual-band filter is realized by designing two individual bandpass filters, each operates on different frequency band, and connecting both sides of these two filters together by two Tjunctions [\[46\]](#page-138-0). Using basic structure of bandstop filter with multiple shunt stubs with unequal length introduces the dual-band performance with transmission zeros [\[47\]](#page-138-0), [\[48\]](#page-138-0), stepped impedance resonator has been a successful approach [\[49–52\]](#page-138-0), however it suffers from high losses, many other dual-band resonators and filter have been introduced in the recent years, we will discuss about them in details in the next chapters.

### 1.4 Contributions and Thesis Organization

The outlines of the thesis and authors contributions are organized as the following:

Chapter 2 consists of two parts, in the first part we are going to give a brief introduction to filer design theory. Second part gives a brief introduction to the different planar techniques.

Chapter 3 discusses quasi-lumped elements that are built on multilayer transmission line, in the first section we will give a brief introduction about the multilayer transmission lines, their characteristic impedance, and the capacitive coupling that these transmission lines provide by making use of both sides of the substrate. The second section discusses the realization of quasi-lumped elements and quasi-lumped resonators using these multilayer transmission lines. Section 3.3 introduces a coplanar waveguide lowpass filter using this technology, while section 3.4 introduces a compact quasi-lumped microstrip bandpass filter using these transmission lines. The same filter is reconstructed in section 3.5 to realize a coplanar waveguide bandpass filter. In section 3.6 the same filter is used as microstrip-CPW transition in addition to its filtering function. Section 3.7 introduces a simple ultra-wideband bandpass filter with very wide stopband using suspended stripline.

Chapter 4 investigates defected ground structures (DGS) for microstrip line. At the beginning of the chapter, an introduction to DGS is given. Section 4.1 introduces a compact DGS slot in the shape of interdigital element. Section 4.2 introduces the interdigital slot for lowpass filter application. Section 4.3 investigates of the integration and packaging difficulties of DGS components and proposes a solution for that purpose.

Chapter 5 discusses the dual-mode and multiple-mode resonators and filters. An introduction to the available planar dual-mode resonators is give in this chapter. Section 5.1 introduces a microstrip triple-mode resonator, this resonator is used to design quasi-elliptic bandpass filters with one and three transmission zeros, an equivalent circuit is also proposed. Section 5.2 introduces a compact suspended stripline dual-mode resonator by combining the open-loop resonator with the quasi-lumped parallel resonator.

Chapter 6 investigates dual-band bandpass filters. A brief introduction is given about the available dual-band filter structures in this chapter. Section 6.1 introduces a dual-band bandpass filter by introducing transmission zeros in the passband of broadband bandpass filter using dual-mode resonator. Section 6.2 introduces a suspended stripline dual-band bandpass filter by splitting the modes of the dual-mode resonator that is introduced in section 5.2.

Chapter 7 gives conclusions of this work in addition to some suggestions for future work.

# <span id="page-30-0"></span>Chapter 2 Background

RF filters are two-port networks that provide frequency selectivity for the system. This device is characterized by its amplitude-squared transfer function, which is described mathematically as [\[1\]](#page-134-0)

$$
|s_{21}(j\omega)|^2 = \frac{1}{1 + \varepsilon^2 F_n^2(\omega)},
$$
\n(2.1)

where  $\varepsilon$  is a ripple constant,  $F_n(\omega)$  represents the filtering or characteristic function. It is to let  $\omega$  represents the radian frequency variable of a lowpass filter that has a cut-off frequency at  $\omega = \omega_c$  for  $\omega = 1 \text{ (rad/s)}$ 

Another important parameter that characterizes the two-port network, such as filter, is called group delay, which is describes the actual delay between the input and output signal, it is also called the envelop delay, which is mathematically defined as [\[2\]](#page-134-0)

$$
\tau_g = \frac{d\phi_{S_{21}}}{d\omega},\tag{2.2}
$$

where

$$
\phi_{S_{21}} = ArgS_{21}(j\omega) \tag{2.3}
$$

The locations of the poles and zeros at the complex s-plane are also considered to be important. To be able to find that, we have to define the rational transfer function, which for is defined linear time-invariant network, such as filters, as [\[2\]](#page-134-0)

$$
S_{21}(s) = \frac{N(s)}{D(s)},
$$
\n(2.4)

where  $N(s)$  and  $D(s)$  are polynomials in the complex frequency variable  $s = \sigma + j\omega$ . Where the roots of the numerator are usually the zeros of the transfer function, and the roots of the denominator are the poles.

#### <span id="page-31-0"></span>2.1 Filter Types

The filters are classified into different types depending on their filtering function  $F_n(\omega)$ , which in turn affect the values of elements used in the filter structure to achieve a certain filter response.

#### 2.1.1 Butterworth Response

The frequency response of the Butterworth filter is maximally flat (has no ripples) in the passband, and rolls off towards zero in the stopband. All poles are distributed on a unity circuil on the complex s-plane.The amplitude-square transfer function of filter is given by [\[2\]](#page-134-0)

$$
|s_{21}(j\omega)|^2 = \frac{1}{1 + \omega^{2n}},
$$
\n(2.5)

where  $n$  is the degree (order) of the filter, which corresponds to the number of reactive elements required in the lowpass prototype.Its all stopband zeros (transmission zeros) located at infinity, and the poles are distributed in a circle. .

#### 2.1.2 Chebyshev Response

Chebyshev response has steeper cut-off than that of the maximally flat response, since it exhibits the equi-ripple in the passband. The amplitude-square transfer function of the filter is given by [\[2\]](#page-134-0)

$$
|s_{21}(j\omega)|^2 = \frac{1}{1 + \varepsilon^2 T_n^2(\omega)},
$$
\n(2.6)

where the ripple constant  $\varepsilon$  is related to a given passband ripple  $L_{Ar}$  in dB by

$$
\varepsilon = \sqrt{10^{\frac{L_{Ar}}{10}} - 1} \tag{2.7}
$$

 $T_n(\omega)$  is the chebyshev function of order n and defined as

$$
T_n(\omega) = \begin{cases} \cos(n \cos^{-1} \omega), & |\omega| \le 1 \\ \cosh(\cosh^{-1} \omega), & |\omega| \ge 1 \end{cases}
$$
 (2.8)

The same as in the case of butterworth, all transmission zeros are located at infinity, while all poles are distributed on an ellipse in the complex s-plane. Because of the passband ripple, the response of the filter has smoother response in the passband than in the case of Butterworth.

Another filter response related to Chebyshev function is called Chebyshev Type II Filter, also known as the Inverse Chebyshev Filter, the reason for naming it is called like this because its response is the inverse of the Chebyshev filter response. The amplitude-sqare transfer function is given as [\[53\]](#page-138-0),

$$
|s_{21}(j\omega)|^2 = \frac{1}{1 + \frac{1}{\varepsilon^2 T_n^2(\frac{1}{\omega})}}
$$
(2.9)

<span id="page-32-0"></span>In contrary to the chebyshev filter, this response is maximally flat at passband and exhibits equi-ripple at the stopband.

#### 2.1.3 Elliptic Response

It is also called Chebyshev-Cauer response. This kind of filters has equi-ripple at their passband and the stopband. The amplitude-squared transfer function is given in [\(2.1\)](#page-30-0). Where  $F_n(\omega)$  is the filtering function and it is given as [\[1\]](#page-134-0)

$$
F_n(\omega) = \begin{cases} M \frac{\prod_{i=1}^{\frac{n}{2}} (\omega_i^2 - \omega^2)}{\prod_{i=1}^{\frac{n}{2}} (\omega_i^2 - \omega^2)}, & n = \text{even} \\ N \frac{\prod_{i=1}^{\frac{n-1}{2}} (\omega_i^2 - \omega^2)}{\prod_{i=1}^{\frac{n-1}{2}} (\frac{\omega_i^2}{\omega_i^2} - \omega^2)}, & n \ge 3 \qquad \text{(odd)}, \end{cases} (2.10)
$$

where  $\omega_s$  is the stopband frequency, which is greater than one, M and N are constants.

## 2.2 Elements Realization for Lowpass Prototype Filters

The definition of the lowpass prototype filter is that filter whose elements are so normalized to make the source impedance equal to one, that is denoted as  $g_0 = 1$ , and the cut-off frequency to be unity, which is denoted as  $\omega_c = 1 (rad/s)$ .

Fig. [2.1](#page-33-0) shows two forms of lowpass prototype filter, each of the forms is dual to each other and give the same response, therefore, both structures can be used. It should be known that  $n$  is the order of the filter or the number of the reactive elements in the filter structure, thus,  $g_o, g_{n+1}$  represent the source and load impedances. This is also valid for even order filter form that is shown in Fig[.2.2](#page-33-0)

These lowpass forms serve as a prototype for designing many practical filters with their cut-off frequency and element transformations. Therefore, it is important to study this prototype for the known filtering functions.

#### 2.2.1 Butterworth Lowpass Prototype Filters

The values of electric elements of the butterworth response with cut-off frequency  $\omega_c = 1$  at insertion loss  $L_{Ar} = 3.01$ , can be easily done by applying [\[1\]](#page-134-0)

$$
g_o = g_{n+1} = 1,\t\t(2.11)
$$

$$
g_i = 2\sin\left(\frac{\pi(2i-1)}{2n}\right), \quad \text{for} \quad i = 1 \quad \text{to} \quad n,\tag{2.12}
$$

<span id="page-33-0"></span>

Figure 2.1: Two forms of odd order lowpass prototype filter, inductance as first element (up), capacitance as first element (down).



Figure 2.2: Two forms of even order lowpass prototype filter, inductance as first element (up), capacitance as first element (down).

From these two equations, we can notice that butterworth filter is always symmetrical network, which means that  $g_1 = g_{n+1}, g_2 = g_n$  and so on. The higher the order of the filter is the higher the steepness of the cut-off slope, and the better the rejection at the stopband is. Thus, increasing the order of the filter or the user reactive elements would lead to better filter, the relation between  $n$  and the stopband attenuation can be written as

$$
n \ge \frac{\log(10^{0.1L_{AS}} - 1)}{2 \log \omega_s},
$$
\n(2.13)

where  $L_{AS}$  is the stopband attenuation in dB at  $\omega_s$ .

#### 2.2.2 Chebyshev Lowpass Prototype Filters

Similarly, chebyshev response can be easily realized by reactive elements by applying the following equations [\[5\]](#page-134-0).

$$
g_o = 1,\tag{2.14}
$$

$$
g_1 = \frac{1}{\gamma} \sin\left(\frac{\pi}{2n}\right),\tag{2.15}
$$

<span id="page-34-0"></span>
$$
g_i = \frac{1}{g_{i-1}} \frac{4 \sin\left(\frac{\pi(2i-1)}{2n}\right) \sin\left(\frac{\pi(2i-3)}{2n}\right)}{\gamma^2 + \sin^2\left(\frac{\pi(2i-1)}{n}\right)}, \quad \text{for} \quad i = 2 \quad \text{to} \quad n,
$$
 (2.16)

$$
g_{n+1} = \begin{cases} 1, & n \quad \text{odd} \\ \coth^2\left(\frac{\beta}{4}\right), & n \quad \text{even}, \end{cases}
$$
 (2.17)

where,

$$
\beta = \ln\left(\coth\left(\frac{L_{Ar}}{17.37}\right)\right),\tag{2.18}
$$

$$
\gamma = \sinh\left(\frac{\beta}{2n}\right),\tag{2.19}
$$

The order of the filter can be simply calculated by applying the following equation

$$
n \ge \frac{\cosh^{-1} \sqrt{\frac{10^{0.1L_{As}} - 1}{10^{0.1L_{Ar}} - 1}}}{\cosh^{-1}(\omega_s)},
$$
\n(2.20)

where  $L_{As}$ ,  $L_{Ar}$  are the minimum stopband rejection and the various ripple at the passband in dB, respectively.

#### 2.2.3 Elliptic Lowpass Prototype Filters

Elliptic filters has equal-ripple at the passband and stopband, which means that this filter has similar response at the passband that chebyshev has, therefore it is called chebyshev- cauer filter. Elliptic lowpass prototype filter is realized by implementing either parallel resonator instead of series inductor as it is shown in Fig. [2.3,](#page-35-0) or by implementing series resonator instead of shunt capacitance as shown in Fig. [2.4.](#page-36-0) Unfortunately, there is no simple equation to realize the values of the elliptic lowpass filter elements as in the case of chebyshev and butterworth, but still there are some tables of the normalized filter element values [\[1\]](#page-134-0),[\[2\]](#page-134-0).

A simple realization for similar response can be realized by computing the elements of chebyshev prototype for the desired cut-off. Then replacing either parallel resonator instead of series resonator, or by implementing series resonator instead of shunt capacitance. This response is called quasi-elliptic filter response. Now, the values of the resonator elements can be calculated. For the first case where we have implemented parallel resonator instead of series inductance, at the cut-off frequency, the impedance of the resonator should be equal to the impedance of the original inductance. While, at attenuation pole (transmission zero), the admittance of the parallel resonator is equal to zero, which can be written as,

$$
\frac{1}{j\omega_c C^e + \frac{1}{j\omega_c L^e}} = j\omega_c L,\tag{2.21}
$$

$$
j\omega_z C^e + \frac{1}{j\omega_z L^e} = 0,\t\t(2.22)
$$

<span id="page-35-0"></span>where  $C_e$  and  $L^e$  are the capacitive and inductive values of the resonator, respectively,  $\omega_z$  is the angular frequency at the desired transmission zero,  $\omega_c$  is the angular cut-off frequency, and L is the inductive value of the original chebyshev element.

For the second case, where we have implemented a series resonator instead of the shunt capacitance in the original chebyshev lowpass filter, similar to the first realization the impedance of the resonator is equal to zero at the transmission zero frequency, and the impedance of the resonator should be equal to the impedance of the original shunt capacitance, which can be written as,

$$
j\omega_z L^e + \frac{1}{j\omega_z C^e} = 0,
$$
\n(2.23)

$$
j\omega_c L^e + \frac{1}{j\omega_c C^e} = \frac{1}{j\omega_c C},\qquad(2.24)
$$

where  $C_e$  and  $L^e$  are the capacitive and inductive values of the resonator, respectively,  $\omega_z$  is the angular frequency at the desired transmission zero,  $\omega_c$  is the angular cut-off frequency, and C is the capacitive value of the original Chebyshev element.



Figure 2.3: Elliptic lowpass prototype filter by using parallel resonators, even order (up), odd order (down).

#### 2.2.4 Elements Transformations

The actual value of the lowpass filter elements are depending on the source impedance, cut-off frequency, and the normalized elements that have been described in this section. Having all these parameters, the actual element values can be formed as [\[1\]](#page-134-0)

$$
L_i = \frac{g_i Z_0}{\omega_c},\tag{2.25}
$$
<span id="page-36-0"></span>

Figure 2.4: Elliptic lowpass prototype filter by using series resonators, even order (up), odd order (down).

$$
C_i = \frac{g_i}{Z_0 \omega_c},\tag{2.26}
$$

where  $C_i$  and  $L_i$  are the capacitive and inductive values of the lowpass filter, respectively,  $Z_0$  is the source impedance, and  $\omega_c$  is the cut-off frequency.

For filters in microwave range the lumped elements are replaced by distributed elements, where their values can only be approximated. For this reason the achieved microwave filter responses do not fully agree with the prototype responses, therefor these filters are called quasi-chebyshev, quasi-butterworth or quasi-elliptic responses.

### 2.3 Bandpass Transformation

Lowpass to bandpass transformation can be achieved by transforming  $\omega$  to  $\omega$ , where  $\omega'$  is defined as [\[54\]](#page-138-0)

$$
\omega' = \alpha \left( \frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \right),\tag{2.27}
$$

where

$$
\alpha = \frac{1}{FBW} = \frac{\omega_0}{\omega_2 - \omega_1},\tag{2.28}
$$

where FBW is the fractional bandwidth of the bandpass filter,  $\omega_2$ ,  $\omega_1$  are the upper and lower edges of the bandpass filter, respectively, and  $\omega_0$  is the center frequency of the filter that is mathematically defined as [\[54\]](#page-138-0)

$$
\omega_0 = \sqrt{\omega_1 \omega_2} \tag{2.29}
$$

Applying this transformation to the impedance  $Z$  of the series inductance  $L$  we obtain [\[54\]](#page-138-0)

$$
Z = jL\omega \Longrightarrow jL\alpha \left(\frac{\omega}{\omega_0} - \frac{\omega_0}{\omega}\right) = j\left(\frac{L\alpha}{\omega_0}\right)\omega - \frac{j}{\omega\left(\frac{1}{L\alpha\omega_0}\right)}\tag{2.30}
$$

The resulting impedance is an impedance of a series resonator with inductive value

$$
L' = \frac{L\alpha}{\omega_0},\tag{2.31}
$$

and capacitive value

$$
C' = \frac{1}{L\alpha\omega_0} \tag{2.32}
$$

Similarly, applying the same transformation for the admittance Y of shunt capacitance C, the resulting admittance is then an admittance of a parallel resonator with inductive value [\[54\]](#page-138-0)

$$
L' = \frac{1}{C\alpha\omega_0} \tag{2.33}
$$

and capacitive value

$$
C' = \frac{C\alpha}{\omega_0} \tag{2.34}
$$

The resulting bandpass structure is shown in Fig. 2.5



Figure 2.5: Bandpass filter prototype.

Due to the difficulty of achieving this bandpass filter prototype using the available technologies, immittance inverters may be used to overcome this problem. Immittance inverters are classified into either impedance or admittance inverter. An ideal immittance inverter is a two-port network having a unique property at all frequencies, so if an impedance  $Z_2$  terminates one port, the impedance  $Z_1$  seen looking at the other port as [\[2\]](#page-134-0)

$$
Z_1 = \frac{K^2}{Z_2},\tag{2.35}
$$

Where  $K$  is the characteristic impedance of the inverter.

The same is for the admittance inverter, so if an admittance  $Y_2$  is connected to one port, the admittance  $Y_1$  seen looking at the other port as

$$
Y_1 = \frac{J^2}{Y_2},\tag{2.36}
$$

where J is the characteristic admittance of the inverter.

An important characteristic of the inverter is that it has a phase shift of  $\pm 90$  and its odd multiple [\[1\]](#page-134-0).

To use these inverters in filter design we should know first that, a series inductance with an inverter on each side looks like a shunt capacitance from the output side as shown in Fig.2.6. Similarly, a shunt capacitance with an inverter on each side looks like series inductance as shown in Fig.2.7. It should also be known that the inverters have the ability to shift the impedance or the admittance depending on the value of the  $K, J$  parameters. Using the knowledge of these parameters enables us to convert a filter circuit to an equivalent form, which would be more convenient for implementation with microwave filters especially for bandpass filters, since both series and shunt resonators are not always available. A series resonator connected by impedance inverters from both sides looks like shunt resonator, and a shunt resonator connected by admittance inverters looks like series resonator



Figure 2.6: Admittance inverters used to convert a series inductance into its equivalent circuit with shunt capacitance.



Figure 2.7: Admittance inverters used to convert a shunt capacitance into its equivalent circuit with series inductance.

To design a bandpass filter using the immittance inverters, it is effective to start from the lowpass filter. Fig[.2.8](#page-39-0) shows a lowpass filter using impedance inverters, similarly, Fig[.2.9](#page-39-0) shows a lowpass filter using admittance inverters. The values of the inductive and capacitive values of the filter can be arbitrary chosen, and then the  $K$ , J parameters are [\[2\]](#page-134-0)

$$
K_{0,1} = \sqrt{\frac{Z_0 L_{s1}}{g_0 g_1}},\tag{2.37}
$$

$$
K_{i,i+1} = \sqrt{\frac{L_{si}L_{si_1}}{g_i g_{i+1}}}, \text{ for } i = 1 \text{ to } n-1,
$$
 (2.38)

<span id="page-39-0"></span>
$$
K_{n,n+1} = \sqrt{\frac{L_{sn} Z_{n+1}}{g_n g_{n+1}}},\tag{2.39}
$$

$$
J_{0,1} = \sqrt{\frac{Y_0 C_{s1}}{g_0 g_1}},\tag{2.40}
$$

$$
J_{i,i+1} = \sqrt{\frac{C_{si}C_{si}}{g_ig_{i+1}}}, \text{ for } i = 1 \text{ to } n-1,
$$
 (2.41)

$$
J_{n,n+1} = \sqrt{\frac{C_{sn}Y_{n+1}}{g_n g_{n+1}}},\tag{2.42}
$$

where  $g_i$  are the values of the original prototype elements,  $Z_0$ ,  $Y_0$  are the generator impedance and admittance, respectively, and  $Z_{n+1}$ ,  $Y_{n+1}$  are the load impedance and admittance, respectively.



Figure 2.8: Low-pass filter structure using impedance inverters.



Figure 2.9: Low-pass filter structure using admittance inverters .

Since the inverters are frequency invariant, the lowpass to bandpass transformation can be easily done using the element transform that is discussed above. Fig. [2.10](#page-40-0) shows bandpass filters using the impedance inverters connected to series resonators, while the filter shown in Fig. [2.11](#page-40-0) consists of shunt resonators connected to admittance inverters. Since source impedances are the same for filters mentioned in both figures, there is no need for impedance scaling, the scaling factor is then  $\gamma = 1$ , and now the inductance of the lowpass filter will be transformed to a series resonator, then we obtain [\[54\]](#page-138-0):

$$
L_{ai} = \left(\frac{\Omega_c}{FBW\omega_0}\right) L_{si},\tag{2.43}
$$

$$
C_{ai} = \frac{1}{\omega_0^2 L_{si}}\tag{2.44}
$$

<span id="page-40-0"></span>Having transformed the series inductance into series resonator, we can easily transform the K parameter by substituting the value of  $L_s$ , then we get [\[2\]](#page-134-0)

$$
K_{0,1} = \sqrt{\frac{Z_0 F B W L_{a1} \omega_0}{\Omega_c g_0 g_1}},
$$
\n(2.45)

$$
K_{i,i+1} = \frac{FBW\omega_0}{\Omega_c} \sqrt{\frac{L_{ai}L_{a(i+1)}}{g_ig_{i+1}}}, \text{ for } i = 1 \text{ to } n-1,
$$
 (2.46)

$$
K_{n,n+1} = \sqrt{\frac{Z_{n+1} FBW L_{an} \omega_0}{\Omega_c g_n g_{n+1}}},
$$
\n(2.47)



Figure 2.10: Bandpass filter built with impedance inverters and series resonators .



Figure 2.11: Bandpass filter built with admittance inverters and parallel resonators.

Similarly, transformation of the lowpass filter to a bandpass filter using parallel resonator connected to admittance inverters can be easily done in the same way, but in this case, the lowpass filter to be transformed is the one with shunt capacitates connected to admittance inverters, see Fig[.2.9.](#page-39-0)

$$
C_{pi} = \left(\frac{\Omega_c}{FBW\omega_0}\right)C_{si},\tag{2.48}
$$

$$
L_{pi} = \frac{1}{\omega_0^2 C_{pi}}\tag{2.49}
$$

Having transformed the shunt capacitance into parallel resonator, we can easily transform the J parameter by substituting the value of  $C_p$ , then we get

$$
J_{0,1} = \sqrt{\frac{Y_0 F B W C_{p1} \omega_0}{\Omega_c g_0 g_1}},\tag{2.50}
$$

$$
J_{i,i+1} = \frac{FBW\omega_0}{\Omega_c} \sqrt{\frac{C_{pi}C_{p(i+1)}}{g_i g_{i+1}}}, \text{ for } i = 1 \text{ to } n-1,
$$
 (2.51)

$$
J_{n,n+1} = \sqrt{\frac{Y_{n+1}FBWC_{pn}\omega_0}{\Omega_c g_n g_{n+1}}}
$$
\n(2.52)

Since most of the microwave filters are waveguide and planar based it is important that these distributed elements or resonators have the same reactance or susceptance equal to that for LC resonators. Thus, it is important that the reactance/susceptance and the reactance/susceptance slope are equal to their corresponding lumped resonator value at the center frequency. This is however, convenient for narrow band filters. Fig. 2.12 shows a bandpass filter using distributed elements connected to impedance inverters, while, Fig. [2.13](#page-42-0) shows a bandpass filter using distributed elements connected to admittance inverters. The reactance slope for a resonator having zero at the center frequency is

$$
x = \frac{\omega_0}{2} \frac{dX}{d\omega}, \quad \omega = \omega_0,\tag{2.53}
$$

where  $\omega_0$  is the center frequency, and  $X(\omega)$  is the reactance of the distributed resonator. It is known that in the ideal case, the reactive slop parameters of a series resonator is  $\omega_0 L_{ai}$ , so by replacing this value by the  $x_i$  parameters, we can define the impedance inverter as [\[2\]](#page-134-0)

$$
K_{0,1} = \sqrt{\frac{Z_0 F B W x_1 \omega_0}{\Omega_c g_0 g_1}},\tag{2.54}
$$

$$
K_{i,i+1} = \frac{FBW}{\Omega_c} \sqrt{\frac{x_i x_{i+1}}{g_i g_{i+1}}}, \text{ for } i = 1 \text{ to } n-1,
$$
 (2.55)

$$
K_{n,n+1} = \sqrt{\frac{Z_{n+1} F B W x_n \omega_0}{\Omega_c g_n g_{n+1}}},\tag{2.56}
$$



Figure 2.12: Bandpass filter using distributed elements connected to impedance inverters.

The same is valid for the second structure (see Fig[.2.13\)](#page-42-0), the susceptance slope parameters for a resonator having zero at the center frequency is

$$
b = \frac{\omega_0}{2} \frac{dB(\omega)}{d\omega}, \quad \omega = \omega_0,\tag{2.57}
$$

where  $\omega_0$  is the center frequency, and  $B(\omega)$  is the susceptance of the distributed resonator. It is known that in the ideal case, the susceptance slope parameters of a

<span id="page-42-0"></span>

Figure 2.13: Bandpass filter using distributed elements connected to admittance inverters.

parallel resonator is  $\omega_0 C_p$ , so by replacing this value by  $b_i$ , the admittance inverter parameters we can define the as

$$
J_{0,1} = \sqrt{\frac{Y_0 F B W b_1 \omega_0}{\Omega_c g_0 g_1}},\tag{2.58}
$$

$$
J_{i,i+1} = \frac{FBW}{\Omega_c} \sqrt{\frac{b_i b_{i+1}}{g_i g_{i+1}}}, \text{ for } i = 1 \text{ to } n-1,
$$
 (2.59)

$$
J_{n,n+1} = \sqrt{\frac{Y_{n+1} F B W b_n}{\Omega_c g_n g_{n+1}}}.
$$
\n(2.60)

### 2.4 Coupling Matrix and Cross Coupled Resonators

Coupling matrix is a representation of the filter that describes the coupling between the resonators of a certain filter with certain bandwidth and center frequency, regardless of the nature of the coupling between the resonators. Fig. 2.14 shows the bandpass filter with n-coupled resonators, where  $R, C$ , and  $L$  are resistance capacitance and inductance, respectively.  $i$  is the current and  $e_s$  is the voltage source. The coupling between one resonator and all other resonators is allowed.



Figure 2.14: n-coupled resonators [\[2\]](#page-134-0).

Using the voltage law, that is the sum of the voltage around any closed circuit must be zero. This low is called Kirchhoff's second law. Applying it for our case will results with [\[2\]](#page-134-0)

$$
(R_1 + jL_1\omega + \frac{1}{jC_1\omega})i_1 - jL_{12}i_2..... - jL_{1n}i_n = e_s
$$
  
\n
$$
-jL_{21}i_1 + (jL_2\omega + \frac{1}{jC_2\omega})i_2..... - jL_{2n}i_n = 0
$$
  
\n
$$
-jL_{n1}i_n - jL_{n2}i_n + .....(jL_n\omega + \frac{1}{jC_n\omega} + R_n)i_n = 0,
$$
\n(2.61)

where  $L_{ij}$  is the mutual coupling between the resonators. The resulting equations can be written in matrix form as [\[2\]](#page-134-0),

$$
[\mathbf{z}][\mathbf{i}] = [\mathbf{e}],\tag{2.62}
$$

where  $[\mathbf{z}]$  is  $(N \times N)$  impedance matrix,  $[\mathbf{i}]$  is the current vector, and  $[\mathbf{e}]$  is the voltage vector. For this case, let us assume that all resonators have the same resonance frequency, which means that the inductive and capacitive values of all resonators have the same values, let it be L for the inductance and C for the capacitance. Now the impedance matrix can be written as [\[2\]](#page-134-0),

$$
[\mathbf{z}] = \omega_0 L F B W \overline{[\mathbf{Z}]},\tag{2.63}
$$

where FBW is the fractional bandwidth and  $\overline{Z}$  is the normalized impedance matrix, which can be written as [\[2\]](#page-134-0)

$$
\overline{\left[\mathbf{Z}\right]} = \begin{pmatrix} \frac{R_1}{\omega_0 L F B W} + p & -j \frac{\omega L_{12}}{\omega_0 L} \frac{1}{F B W} & \dots & -j \frac{\omega L_{1n}}{\omega_0 L} \frac{1}{F B W} \\ -j \frac{\omega L_{21}}{\omega_0 L} \frac{1}{F B W} & p & \dots & -j \frac{\omega L_{2n}}{\omega_0 L} \frac{1}{F B W} \\ \vdots & \vdots & \ddots & \vdots \\ -j \frac{\omega L_{n1}}{\omega_0 L} \frac{1}{F B W} & -j \frac{\omega L_{n2}}{\omega_0 L} \frac{1}{F B W} & \dots & \frac{R_n}{\omega_0 L F B W} + p \\ \vdots & \vdots & \ddots \end{pmatrix} \tag{2.64}
$$

where,

$$
p = j\frac{1}{FBW} \left(\frac{\omega}{\omega_0} - \frac{\omega_0}{\omega}\right),\tag{2.65}
$$

the external quality factor is defined as

$$
Q_{ei} = \frac{\omega_0 L}{R_i},\tag{2.66}
$$

where  $i = 1, \ldots, n$ , Defining the coupling coefficient as

$$
M_{ij} = \frac{L_{ij}}{L},\tag{2.67}
$$

and assuming  $\omega/\omega_0 \approx 1$  for narrow band, we get

$$
\overline{[\mathbf{Z}]} = \begin{pmatrix} \frac{1}{q_{e1}} + p & -jm_{12} & \dots & -jm_{1n} \\ -jm_{21} & p & \dots & -jm_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ -jm_{n1} & -jm_{n2} & \dots & \frac{1}{q_{en}} + p \\ \vdots & \vdots & \ddots & \vdots \\ 0 & \dots & \vdots & \vdots \\ 0
$$

where  $q_{e1}$  and  $q_{en}$  are the scaled external quality factors and defined as

$$
q_{ei} = Q_{ei} FBW,
$$
\n<sup>(2.69)</sup>

and  $m_{ij}$  is the normalized coupling coefficient which is defined as

$$
m_{ij} = \frac{M_{ij}}{FBW},\tag{2.70}
$$

$$
S_{21} = \frac{b_2}{a_1} \mid_{a_2=0} = \frac{2\sqrt{R_1 R_n} i_n}{e_s},\tag{2.71}
$$

$$
S_{11} = \frac{b_1}{a_1} \mid_{a_2=0} = 1 - \frac{2R_1 i_1}{e_s},\tag{2.72}
$$

where

$$
i_1 = \frac{e_s}{\omega_0 L.FBW} [\bar{Z}]_{11}^{-1},\tag{2.73}
$$

$$
i_n = \frac{e_s}{\omega_0 L.FBW} [\bar{Z}]_{n1}^{-1},
$$
\n(2.74)

substituting  $(2.73)$  in  $(2.71)$  and  $(2.74)$  in  $(2.72)$  then

$$
S_{21} = \frac{2}{\sqrt{q_{e1}q_{en}}} [\bar{\mathbf{Z}}]_{n1}^{-1}
$$
 (2.75)

and

$$
S_{11} = 1 - \frac{2}{q_{e1}} [\bar{\mathbf{Z}}]_{11}^{-1}
$$
 (2.76)

the coupling coefficients for coupling structure with resonators having different resonant frequency are

$$
M_{ij} = \frac{L_{ij}}{\sqrt{L_i L_j}}, \qquad i \neq j,
$$
\n(2.77)

which leads to

$$
\overline{[\overline{\mathbf{Z}}]} = \begin{pmatrix} \frac{1}{q_{e1}} + p - m_{11} & -jm_{12} & \dots & -jm_{1n} \\ -jm_{21} & p - m_{22} & \dots & -jm_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ -jm_{n1} & -jm_{n2} & \dots & \frac{1}{q_{en}} + p - m_{nn} \end{pmatrix}
$$
(2.78)

The same can be applied for the case of capacitive coupling between the resonators, but instead of using the impedance matrix  $[\mathbf{Z}]$ , the admittance matrix  $[\mathbf{Y}]$  is used, we will not go through the derivations, nevertheless, the transfer function and the return loss can be written as

$$
S_{21} = \frac{2}{\sqrt{q_{e1}q_{en}}} [\bar{Y}]_{n1}^{-1},
$$
\n(2.79)

and

$$
S_{11} = \frac{2}{q_{e1}} [\bar{Y}]_{11}^{-1} - 1
$$
\n(2.80)

The most important point needed is that the formulation of the normalized impedance matrix  $[Z]$  to that of the normalized  $[Y]$ . So we can generalize coupling between the resonators no matter what the coupling nature is, by

$$
S_{21} = \frac{2}{\sqrt{q_{e1}q_{en}}} [A]_{n1}^{-1},
$$
\n(2.81)

and

$$
S_{11} = \pm \left(\frac{2}{q_{e1}} [A]_{11}^{-1} - 1\right),\tag{2.82}
$$

where  $[A]$  is  $N \times N$  matrix and formed as

$$
[A] = [q] + p[U] - j[m], \tag{2.83}
$$

where [q] is  $(N \times N)$  matrix with all entries zeros except  $q_{11} = 1/q_{e1}$  and  $q_{nn} = 1/q_{en}$ , [U] is  $(N \times N)$  unit matrix, and [m] is  $(N \times N)$  coupling matrix

### 2.5 Planar Transmission Lines

A planar transmission line is a transmission line with multiple conducting metal strips lying in parallel planes. These planes are mostly placed on dielectric material. The most widely used transmission lines are microstrip line, coplanar waveguide, and suspended stripline.

### 2.5.1 Microstrip Line

Microstrip line is a transmission line which consists of a conducting strip separated from a ground plane by a dielectric layer. Fig.2.15 shows the cross section of the microstrip line. The main advantages of microstrip line are that it is suitable technique for MICs, and the radiation that it provides can be used for antenna design. The main disadvatage of this type of transmission lines is that via holes are necessary in the case of shunt connections which is complex especially in the case of MMICs.

The characteristic impedance of the microstrip line is depending on the width of the guided wave line, substrate thickness, and the effective dielectric constant of the substrate  $\varepsilon_r$ . The effective dielectric constant is given in the following form [\[55–](#page-138-0)[57\]](#page-139-0)



Figure 2.15: Microstrip line cross section.

$$
\varepsilon_{eff} = \frac{\varepsilon_r + 1}{2} + \frac{\varepsilon_r - 1}{2\sqrt{1 + \frac{10h}{w}}},\tag{2.84}
$$

<span id="page-46-0"></span>where  $\varepsilon_r$  and h are the permittivity and thickness of the substrate, respectively, and  $w$  is the strip width, the characteristic impedance of the microstrip is given as

$$
Z_c = \frac{\eta}{2\pi\sqrt{\varepsilon_{eff}}} \ln\left(\frac{Fw}{h} + \sqrt{1 + (\frac{2w}{h})^2}\right),\tag{2.85}
$$

where  $\eta = 120\pi\Omega$ , and

$$
F = 6 + (2\pi + 6) \exp\left(-\left(\frac{30.666w}{h}\right)^{0.7528}\right)
$$
 (2.86)

### 2.5.2 Coplanar Waveguide

Coplanar waveguide (CPW) is basically a single strip located between two ground planes on the same side of the substrate, see Fig. 2.16. The main advantages for this type of transmission lines is thae fact that it can be easily integrates with the MIC's. Furthermore shunt connections can be easily realized without the need of via holes. in addition it is less sensitive to the substrate thickness than in the case of microstrip [\[58\]](#page-139-0). However the losses in this transmission line are higher than that in the case of microstrip lines. Both ground planes must be at the same potential, to avoid the asymmetric, which may excites the slot mode. Therefore air bridges are used to keep symmetrical potential at both ground planes.



Figure 2.16: Coplanar waveguide cross section.

The characteristic impedance of the coplanar waveguide with finite substrate thickness is given by [\[58\]](#page-139-0),

$$
Z_c = \frac{f(K)}{4} \sqrt{\frac{\mu_0}{\varepsilon_0 \varepsilon_{eff}}},\tag{2.87}
$$

where,

$$
\varepsilon_{eff} \approx 1 + \frac{\varepsilon_r - 1}{2} f(K1) f(K),\tag{2.88}
$$

$$
K = \frac{w}{w + 2s},\tag{2.89}
$$

$$
K_1 = \sqrt{\frac{1}{1+q}},\tag{2.90}
$$

$$
q = \frac{\left[\sinh\left(\frac{w\pi}{4h}\right)\right]^2}{\sinh\left(\frac{s\pi}{2h}\right)\sinh\left(\frac{\pi(w+s)}{2h}\right)},\tag{2.91}
$$

$$
f(K) = \begin{cases} \frac{1}{4} \ln \left( \frac{2}{\sqrt{K}} \right), & K \le 0.173\\ \frac{\pi}{\ln \left( 2 \frac{1 + \sqrt{K}}{1 + \sqrt{K}} \right)}, & K \ge 0.173, \end{cases}
$$
(2.92)

where h is the substrate thickness,  $w$  is the width of the transmission line, and s is the spacing between the transmission line and the ground planes.

#### 2.5.3 Suspended Stripline

Suspended stripline (SSL) has been introduced as an alternative to coaxial line in [\[59\]](#page-139-0). It is basically a substrate that is shielded inside a housing mount, as it is shown in Fig. 2.17. Suspended stripline is also possible with multiple substrates [\[60–64\]](#page-139-0). The ground plane of this transmission line is the mount itself. Due to the existence of the mount around the guided wave line, there is no radiation loss introduced by this transmission line. SSL has another main advantage, which is due to the ability of building the resonators on both sides of the substrate, it is the most suitable technique for broadband circuits [\[24,](#page-136-0) [40,](#page-137-0) [65\]](#page-139-0). Due to the larger cross section with a considerable amount of electromagnetic field in the air, the effective dielectric constant of the SSL is rather low, and therefore the dielectric loss is very low in this transmission line.



Figure 2.17: Suspended stripline cross section.

Since most MICs are microstrip based, there might be a need to integrate the SSL filters with microstrip components. That can be realized by having a grove under the portion of the filter in the carrier block of the circuit and fixing a small cap over the SSL filter to build the channel of the filter, see [\[66\]](#page-139-0). The characteristic impedance, and the effective dielectric constant of the SSL are given as [\[67\]](#page-139-0), [\[68\]](#page-139-0),

• When  $0 < w < a/2$ 

$$
Z_c = \frac{\eta_0}{2\pi} \Big[ V + R \ln \Big( \frac{6}{w/b} + \sqrt{1 + \frac{4}{w/b}} \Big) \Big],
$$
 (2.93)

$$
\varepsilon_{eff} = \frac{1}{\left(E - F \ln \frac{w}{b} \frac{1}{\sqrt{\epsilon_r}}\right)^2},\tag{2.94}
$$

where  $w$  is the width of the transmission line,  $a$  is the width of the mount,  $b$  is the hight of the mount,

$$
V = 1.7866 + 0.2035 \frac{h}{b} + 0.4750 \frac{a}{b},\tag{2.95}
$$

$$
R = 1.0835 + 0.1007 \frac{h}{b} - 0.09457 \frac{a}{b},\tag{2.96}
$$

$$
E = 0.2077 + 1.2177 \frac{h}{b} - 0.08364 \frac{a}{b},\tag{2.97}
$$

$$
F = 0.03451 - 0.1031 \frac{h}{b} + 0.01742 \frac{a}{b},\tag{2.98}
$$

•  $\frac{a}{2}$  < w < a

$$
Z_c = \eta_0 \left( V + \frac{R}{\frac{w}{b} + 1.393 + 0.6670 \ln\left(\frac{w}{b} + 1.444\right)} \right),\tag{2.99}
$$

$$
\varepsilon_{eff} = \frac{1}{\left(E - F \ln \frac{w}{b} \frac{1}{\sqrt{\epsilon_r}}\right)^2},\tag{2.100}
$$

where,

$$
V = -0.6301 - 0.07083 \frac{h}{b} + 0.247 \frac{a}{b},\tag{2.101}
$$

$$
R = 1.9492 + 0.1553 \frac{h}{b} - 0.5123 \frac{a}{b},\tag{2.102}
$$

$$
E = 0.464 + 0.9647 \frac{h}{b} - 0.2063 \frac{a}{b},\tag{2.103}
$$

$$
F = -0.1424 + 0.3017 \frac{h}{b} - 0.02411 \frac{a}{b}
$$
 (2.104)

### 2.5.4 Multilayer Transmission Lines

Multilayer transmission lines are mainly introduced for MMIC's. It is basically a combination of CPW and microstrip line, this structure is built on a thin film placed on a thick substrate, fabrication, however, is very expensive since Si, Ge, or GaAs is used. The main advantage of this techniques is that it can be easily integrated with CPW and microstrip components. It also provide high coupling between the resonators, which makes it useful for broadband components [\[40\]](#page-137-0), [\[69](#page-139-0)[–72\]](#page-140-0).

## Chapter 3

# Multilayer Structures and Filter Applications

Multilayer structures represent a potential technology for MMIC and MIC circuits [\[69–](#page-139-0)[72\]](#page-140-0) and [\[73\]](#page-140-0). These structures were introduced as a good candidate for filter applications in [\[70\]](#page-140-0). They offer a wider range for nearly constant characteristic impedance and provide more effective capacitive coupling between the resonators by locating them on the two sides of the substrate [\[70\]](#page-140-0), [\[72\]](#page-140-0).

Multilayer structures are normally used for coplanar waveguide (CPW), Microstrip line (ML), and suspended stripline (SSL) techniques. They give the designer extra degree of freedom in designing the microwave and millimeter wave components. The multilayer structures for CPW are normally built on a thin film structure, where the metallization strips and ground planes are etched [\[72\]](#page-140-0). In case of high frequency components, the material that is used for the thin film is silicon dioxide  $SiO<sub>2</sub>$  [\[74\]](#page-140-0), [\[75\]](#page-140-0). The thin film is then built over high resistivity silicon substrate. This process is ,however, a complicated process rather expensive.

This chapter investigates the cross section of multilayer structure and introduces different filters using this technology. Compact lowpass and bandpass filters are designed using this technology showing the ability of these filters to be integrated with ML, CPW, or both. The filter are designed using quasi-lumped elements. In the last section an ultra-wideband suspended stripline filter is presented. The filter has very wide stopband which is much wider than that for the other available structures, in addition the filter has low group delay variation with the passband.

### 3.1 Multilayer Coplanar Line Cross Section

The multilayer coplanar line (MCL) of a modified cross section is investigated in this section. Fig. [3.1](#page-51-0) shows the cross section of the proposed MCL. Only one substrate is used and the filter is built on both sides of it. Fig. [3.1a](#page-51-0) shows the MCL cross section which is used in the case of broadside coupling, by this configuration high capacitive <span id="page-51-0"></span>coupling can be achieved, since it allows the overlapping between the metallization on both sides of the substrate. This structure can be easily integrated with both CPWand microstrip-based circuits, depending on which side of the substrate these circuits are built. This is not the case with the standard microstrip and CPW lines, as these technologies need transition networks to be integrated together. Fig. 3.1b shows the cross section of the MCL, which is designed to be integrated with the standard CPW. Fig. 3.1c shows the cross section of the line that is compatible with the microstrip line.



Figure 3.1: (a) Cross section of MCL , (b) the MCL compatible with CPW , (c) the MCL compatible with microstrip line .

A comparison is made on the capacitive coupling between 50  $\Omega$  microstrip line, CPW, and MCL broadside coupling. The 50  $\Omega$  lines were built on a AR600 substrate 0.787 mm in thickness with relative permittivity  $\varepsilon_r$  of 6, as shown in Fig. [3.2.](#page-52-0) The study is done on frequency band of 6 GHz. The capacitive values of these structures are calculated in two steps. First, the reflection coefficient of the coupling structure  $S_{11}$  were computed at certain frequencies. In the second step, the coupling structure is considered equivalent to a series capacitance, whose reactance  $X_i$  can be calculated from

$$
S_{11} = \frac{jX_i - Z_0}{jX_i + Z_0},\tag{3.1}
$$

where  $z_i$  is the input impedance - here the load is series capacitance- and  $Z_0$  is the source impedance which is 50  $\Omega$  in our case. Having calculated the load impedance, the capacitive value of the coupling structure can be easily calculated from

$$
C = \frac{-1}{X_i \omega},\tag{3.2}
$$

<span id="page-52-0"></span>where  $w$  is the angular frequency.

Fig. 3.3 shows a comparison between the capacitive values of ML-ML, CPW-CPW and broadside coupling structure as a function of the distance. As it can be clearly seen, the broadside coupling structure provides higher capacitive coupling between the two 50  $\Omega$  lines since it allows the overlapping between the metallization on both sides of the substrate. These coupling structure can be used for broadband circuits and filters.



Figure 3.2: coupling two 50  $\Omega$  lines structure (a) microstrip-microstrip, (b) CPW-CPW, and (c) CPW-slotted microstrip line.



Figure 3.3: Calculated capacitive coupling values between the two ends of 50  $\Omega$ strips of particular lines: CPW- CPW, microstrip-microstrip (ML-ML), and broadside coupling CPW-slotted microstrip line.

In addition to the high capacitive coupling that the MCL offers, it also provides wide characteristic impedance range at the same frequency band. To show that, a simple analysis is done by using the same substrate. The study has been done on the slotted microstrip line (see Fig. [3.1c](#page-51-0)). Fig. 3.4 shows the relation between the characteristic impedance  $Z_0$  of the transmission line and the width of the transmission line w for different slot widths s. As it is shown in the same Figure the impedance  $Z_0$  can reach 135  $\Omega$  with transmission line width equals 0.5 mm and slot width of 4 mm, and 16.2  $\Omega$  with transmission line width of 6 mm and slot width of 1 mm.

Another study has been done on the impedance of the transmission line by changing the width of the ground planes  $a$ , and fixing both the width of the transmission line w and the slot width s at  $2.7 \text{ mm}$  and  $2.8 \text{ mm}$ , respectively, (see Fig. [3.1c](#page-51-0)). Fig. [3.5](#page-54-0) shows the relation between the impedance of the transmission line and the width of the ground planes. From the figure, one can see that the width of the ground plane has almost no effect on the characteristic impedance unless it is less than 2 mm. The characteristic impedance of the transmission line starts increasing by decreasing the width of the ground planes.



Figure 3.4: Characteristic impedance of slotted microstrip line as function of w for different slot width s.

### 3.2 Quasi-Lumped Elements

The quasi-lumped elements are used in the microwave filters due to the advantages they offer. Due to the short transmission line length that is used for quasi-lumped elements, which must be much shorter than quarter-wavelength, the filters designed using these elements have compact size, low losses, and wide stopband [\[24\]](#page-136-0),[\[26\]](#page-136-0), [\[27\]](#page-136-0), and [\[76–78\]](#page-140-0).

<span id="page-54-0"></span>

Figure 3.5: Characteristic impedance of slotted microstrip line as function of the width of the ground plane a.

Since microwave filters require both series and shunt inductances and capacitances and their combination to form either series or parallel resonators, it is necessary to understand how to realize each element for the available transmission lines.

Wide microstrip line and wide CPW line sections with low characteristic impedance already form shunt capacitances. Fig. [3.6](#page-55-0) shows layouts of shunt CPW microstrip line capacitances. In the case of suspended stripline, shunt capacitance is realized by having additional metallization at the backside of the substrate which is connected to the walls of the housing mount from both sides, in addition to the wide transmission line that lies on the topside of the substrate. Fig. [3.7](#page-55-0) shows 3D view for shunt suspended stripline capacitance.

Shunt inductor is realized by connecting a narrow stripline with circuit from one side and to the ground from the other side. In the case of CPW, the ground planes are located near the guided wave line, so realizing shunt inductance can be easily done. It is the same in the case of suspended stripline, the narrow stripline can be shunted by connecting it to the side wall of the housing mount. For microstrip and since the ground plane and guided waveline are built on the opposite sides of the substrate, the narrow stipline is shunted by using via hole, this process is more complicated than in the case of CPW and suspended stripline. Fig. [3.8a](#page-55-0), and Fig. [3.8b](#page-55-0) show the CPW and microstrip shunt inductance, respectively, while Fig. [3.9](#page-56-0) shows 3D view of suspended stripline shunt inductance.

A narrow transmission line that is connected from both sides to the input and output represents series inductance, this applies to CPW, microstrip, and suspended

<span id="page-55-0"></span>

Figure 3.6: Layouts of shunt capacitance for (a) CPW , (b) microstrip.



Figure 3.7: 3D view of suspended stripline shunt capacitance.



Figure 3.8: Layouts of shunt inductance for (a) CPW , (b) microstrip.

<span id="page-56-0"></span>

Figure 3.9: 3D view of suspended stripline shunt inductance.

stripline. The inductive value of this line is depending on the characteristic impedance of the transmission line, the length of the transmission line, and the effective dielectric constant.

Series capacitance is realized by different coupling structures, the first structure is end to end coupling structure [\[2\]](#page-134-0). However, the capacitive value that this structure provides is very low for all transmission line techniques, (see Fig. [3.3,](#page-52-0) and [\[24\]](#page-136-0)). Another coupling structure that is used mainly for CPW, and microstrip line is the interdigital coupling structure as shown in Fig. 3.10, [\[79\]](#page-140-0), [\[80\]](#page-140-0). This structure consists



Figure 3.10: Layout of microstrip interdigital capacitance.

of metallic fingers intersect with each other. This structure provides tight capacitive value, however, the losses of this structure are much higher than the first structure due to the narrow strips used in realizing this structure. For suspended stripline and for multilayer coplanar line, where it is allowed to build the resonators on both sides of the substrate, broadside coupling structures are used. These structures allow overlapping between the resonators, which increases the capacitive coupling between the resonators without increasing the losses on the structure.

### 3.3 Lowpass Filters

Microstrip lowpass filter using multilayer technique has been introduced earlier [\[73\]](#page-140-0). The filter was realized by opening apertures under the narrow transmission lines to increase the inductive values of these transmission line sections. This section deals with CPW lowpass filter built on the same technique, Fig. [3.1.](#page-51-0) The filter shows a great advantage in minimizing the size of the filter, particularly the size of the capacitive line sections. The filter is realized by implementing patches under the capacitive transmission line sections of the classical CPW lowpass filter structure. Since the wide patches increase the capacitive value of the capacitive transmission line sections, shorter capacitive transmission line sections are used. To design a CPW lowpass filter we have to go through two steps:

First, designing a lumped chebyshev lowpass filter, that requires knowing the order, the cut-off frequency, and passband ripple of the filter as described in sec. [2.2.](#page-32-0) Having the order, the cut-off frequency, and passband ripple, the lumped elements of the chebyshev can be simply calculated. As an example, a fifth order chebyshev filter with cut-off frequency of 4 GHz, and passband ripple of 0.1 dB. The normalized elements for this filter are  $g_0 = g_6 = 1$ ,  $g_1 = g_5 = 1.1468$ ,  $g_2 = g_4 = 1.3712$ , and  $g = 1.975$ . Where  $g_0$ , and  $g_6$  represent the source and load impedances, respectively, that is considered for our filter to be  $Z_0 = 50\Omega$ . Substituting these values in [\(2.25\)](#page-35-0), and [\(2.26\)](#page-36-0), the actual filter element values can be calculated, which is for our filter  $C_1 = C_5 = 0.92$  pF,  $L_2 = C_4 = 2.73$  nH, and  $C_3 = 1.57$  pF.

The second step is to realize the desired capacitive and inductive values of the filter elements by the stubs of the high/low-impedance transmission line, the characteristic impedance  $Z_0$  and the effective dielectric constant  $\varepsilon_{eff}$  of the used transmission lines have to be determined. To determine this, a commercial MoM simulator [\[81\]](#page-140-0) is used. By assuming the transmission line lengths of the filter elements are much shorter than the wavelength, the transmission line length can be calculated from

$$
C_k = \frac{l_k}{Z_{0k}v_{ph,k}},\tag{3.3}
$$

$$
L_j = \frac{l_j Z_{0j}}{v_{ph,j}},\tag{3.4}
$$

where the indices  $k$  and j correspond to elements with capacitive and inductive character, respectively.  $C_k$  and  $L_j$  are the capacitance and inductance of the equivalent circuit of the filter, respectively. The phase velocity  $v_{ph}$  is calculated by

$$
v_{ph,j} = \frac{c}{\sqrt{\varepsilon_{eff}}},\tag{3.5}
$$

where  $c$  is the speed of light in the free space.

Having determined all transmission line lengths, these transmission line sections can be combined to build the desired lowpass filter, however, some optimization is needed to take into account the involved discontinuities and to achieve good matching in the passband. The dimensions of the lowpass filter portion are given as part of the overall filter in Fig. 3.11.



Figure 3.11: Top (up) and backside (down) layouts of a CPW lowpass filter, all dimensions are in mm .

A comparison between two filters with the same dimensions is made. The first one is built on one side of the substrate, and the second one having wide patches at the backside of the substrate, as it is shown Fig. [3.12](#page-59-0) the cut-off frequency of the CPW lowpass filter using MCL (with patches at the backside of the substrate) is much lower than that for the CPW classical lowpass filter. That means that adding patches under the capacitive transmission line sections decreases the size of the lowpass filter.

Fig. [3.13](#page-59-0) shows the measured and insertion loss of the lowpass filter, the filter has insertion loss at the passband is better than 0.7 dB, and group delay variation within the passband is about 0.11 ns.

As it is shown in Fig. [3.13,](#page-59-0) the filter has flat cut-off and the rejection at the stopband is about 23.4 dB, which is not sufficient for some applications. Therefore, transmission zeros are needed to increase the rejection at the stopband and to enhance the cut-off sharpness. In order to introduce transmission zeros, the side patches were loaded by two half-wavelength stubs. These stubs are coupled capacitively to the topside of the substrate. Since each of the additional stubs introduces a transmission zero to the filter response at the corresponding frequency, two transmission zeros were introduced by this configuration. Fig. [3.14](#page-60-0) shows the top and backside layouts of the CPW lowpass filter with the additional stubs. Fig. [3.15](#page-61-0) shows the measured and

<span id="page-59-0"></span>

Figure 3.12: Insertion loss of CPW lowpass filter built on one layer of the substrate and Insertion loss of CPW lowpass filter with wide patches under the capacitive transmission line.



Figure 3.13: Measured (solid) and simulated (dashed) insertion and return loss of a CPW lowpass filter with patches.

<span id="page-60-0"></span>simulated insertion and return loss of the filter. The measured insertion loss at the passband is better than 0.5 dB. The measured transmission zeros are located at 5.7 and 6.7 GHz. Good agrement is achieved between the measured and the simulated results except small shift is the location of the transmission zeros, this probably occurs due to fabrication errors.



Figure 3.14: Top (up) and backside (down) layout of the CPW lowpass filter with additional stubs.

## 3.4 Microstrip Bandpass Filters Using Multilayer Line

Using MCL technology and quasi-lumped elements, a bandpass filter compatible with the microstrip line has been designed. The resonators were placed on the backside of the substrate. Fig. [3.16](#page-62-0) shows the layout of the filter. The equivalent circuit model for the proposed structure is shown in Fig. [3.17.](#page-62-0) Each of the two resonant circuits consists of a wide patch capacitively coupled through the substrate to a 50  $\Omega$  microstrip line. This coupling is provided by capacitor  $C_1$ , as shown in Fig. [3.17.](#page-62-0) The narrow strips that are mutually connecting the two patches, (see Fig. [3.17\)](#page-62-0), are represented by the series inductor  $L_3$ . This resonant structure is connected to the ground by another narrow strip represented by the shunt inductor  $L<sub>4</sub>$ . Since the slot between the patch and the ground metallization is narrow, it provides a capacitive coupling between the patch and the ground, which is represented by capacitor  $C_2$ .

The bandwidth of this filter can easily be widened by either narrowing the shunt inductive strips, or by increasing the coupling between the patches and the input/output lines. The center frequency of the filter can be controlled namely by inductive strip

<span id="page-61-0"></span>

Figure 3.15: Measured (solid) and simulated (dashed) insertion and return loss of a CPW lowpass filter with two transmission zeros.

length l, see Fig[.3.16.](#page-62-0) This is documented by the results of a parametric study in Fig. 3.18, where the return loss of the filter for different l is plotted. Increasing l shifts the center frequency of the filter to a lower frequency band, consequently, the bandwidth of the filter is reduced. The structure has been simulated and optimized by the commercial MoM simulator [\[81\]](#page-140-0), and the circuit simulation has been performed on the equivalent circuit using Microwave Office [\[82\]](#page-140-0). Using the circuit topology shown in Fig[.3.17](#page-62-0) and the scattering parameters calculated by the EM simulator for the filter with dimensions shown in Fig. 3.16, the circuit parameters were tuned till a sufficient match between the circuit and the EM analyses was achieved. The resulting circuit parameters are  $C_1 = 0.119$  pF,  $C_2 = 0.105$  pF,  $L_1 = 2.72$  nH, and  $L_2 = 0.407$  nH. Fig[.3.19](#page-63-0) shows the EM and circuit simulations of the filter with dimension shown in Fig[.3.16.](#page-62-0) Fig[.3.20](#page-64-0) shows the simulated and measured insertion and return loss of the filter. The filter has insertion loss at the passband better than 0.9 dB. Very good agreement has been achieved between the EM, circuit simulations and measurement.

A transmission zero was introduced to the filter response by inserting a strong capacitive coupling between the patches. Fig. [3.21](#page-65-0) shows the layout of the filter with the transmission zero, while Fig. [3.22](#page-65-0) shows the equivalent circuit model of this filter. The capacitive coupling between the patches is due to an additional patch located between the 50  $\Omega$  lines on the topside. The slot in this patch is etched to keep the inductances of the strips on the backside at their original value. The patches on the backside were simultaneously widened as it can be observed from a comparison of Fig. [3.16](#page-62-0) with Fig. [3.21.](#page-65-0) This coupling is represented in the equivalent circuit by capacitor  $C_3$ , Fig. [3.22.](#page-65-0) The structure was simulated, optimized and measured.

<span id="page-62-0"></span>

Figure 3.16: Topside (up), and backside (down) layout of an MCL bandpass filter compatible with the microstrip line.



Figure 3.17: Equivalent circuit model of the bandpass filter.

<span id="page-63-0"></span>

Figure 3.18: Simulated return loss of the filter with inductive strip length l vary from 4.7 to 0.6 mm.



Figure 3.19: EM (solid) and Circuit (dashed) simulation of the insertion and return loss of the filter and its equivalent circuit.

<span id="page-64-0"></span>

Figure 3.20: Simulated and measured insertion and return loss of the ML bandpass filter.

The insertion and return losses for the filter are demonstrated in Fig. [3.23.](#page-66-0) The transmission zero is introduced at about 7 GHz. The frequency shift between the simulated and measured data is caused by the discrepancies between the dimensions of the designed and fabricated filter layouts.

### 3.5 CPW Bandpass Filters Using Multilayer Line

In the previous section we have introduced microstrip bandpass filter using the MCL technology. In this section we will introduce the same filter for CPW. To get such a filter, the ground metallization was etched on the topside instead of the backside. By this configuration the filter is now fed by the 50  $\Omega$  CPW. The structure of the resonators was taken from the filter shown in Fig. [3.16.](#page-62-0) The shunt inductor is now connected to the ground via additional patches, which are capacitively coupled through the substrate with the ground planes, as shown in Fig. [3.24.](#page-66-0) These patches are represented in the equivalent circuit of Fig. [3.25](#page-67-0) by capacitor  $C_4$ . Since a shunted series resonator is used instead of the parallel inductance, the transmission zero is generated.

The filter was optimized, fabricated and measured. The area occupied by this filter is nearly the same as the area occupied by the filter shown in Fig[.3.16.](#page-62-0) Fig[.3.26](#page-67-0) shows the simulated and measured insertion and return loss of the filter. The insertion loss at the passband is better than 0.9 dB and the upper stopband rejection better than 26 dB that reachs to higher than 14 GHz. Good agreement has been achieved

<span id="page-65-0"></span>

Figure 3.21: Topside (up), and backside (down) layout of an MCL bandpass filter with additional capacitive coupling between the resonators.



Figure 3.22: Equivalent circuit model of the bandpass filter with additional capacitive coupling between the resonators.

<span id="page-66-0"></span>

Figure 3.23: Measured (solid) and simulated (dashed) insertion and return loss of the microstrip filter with additional transmission zero.



Figure 3.24: Top (up) and backside layouts (down) of an MCL bandpass filter with CPW feed lines,(all dimensions are in mm).

<span id="page-67-0"></span>

Figure 3.25: The equivalent circuit of the of CPW bandpass filter.

between the simulated and measured results.



Figure 3.26: Measured (solid) and simulated (dashed) insertion and return loss of the CPW bandpass filter with transmission zero.

## 3.6 Bandpass Filter with Microstrip-CPW Feed Lines

The bandpass filter introduced in sec[.3.4](#page-60-0) and shown in Fig[.3.16](#page-62-0) has been reconstructed again to achieve a bandpass filter compatible with both CPW and microstrip feed lines. The original filter consists of two wide patches coupled to the input/output 50  $\Omega$  slotted microstrip feed lines. The patches are interconnected by narrow inductive strip, which is grounded at its center by shunt inductive strips. This filter reconstructed to obtain the microstrip-CPW feeding lines. So the ground planes under the original 50  $\Omega$  slotted microstrip feeding line were closed, so the slotted microstrip line was thus replaced by a 50  $\Omega$  microstrip line coupled via a patch. The slotted microstrip line from the other side of the filter was replaced by 50  $\Omega$  CPW line, and a small patch was added on the topside of the substrate to increase the capacitive coupling between the CPW line and the filter itself. The layout of the modified filter is shown in Fig. 3.27, while the simulated insertion and return loss of the filter over wide frequency range are shown in Fig. [3.28.](#page-69-0) the filter has center frequency of 3.55 GHz.



Figure 3.27: Top (up) and backside (down) layouts of a bandpass filter with microstrip-CPW feeding lines.

The filter is designed as a microstrip-CPW transition in addition to its filtering function. As an application to such structure, the filter can be attached to a microstrip antenna that radiates at 3.55 GHz from the microstrip feeding line side. A simple antenna was chosen for this work which is a rectangular patch antenna. The antenna width is chosen to be 15 mm, the length of the antenna can be calculated from [\[83\]](#page-141-0), and [\[84\]](#page-141-0)

$$
L = L_{eff} - 2\Delta L \tag{3.6}
$$

where  $L_{eff}$  is the effective patch length and formed as

$$
L_{eff} = \frac{c}{2f_0\sqrt{\varepsilon_{eff}}}
$$
\n(3.7)

where c is the speed of light in the free space and  $\varepsilon_{eff}$  is the effective dielectric constant that can be calculated from  $(2.84)$ .  $\Delta L$  is the fringing patch length which formed as [\[85\]](#page-141-0)  $\overline{a}$ 

$$
\Delta L = 0.412h \left( \frac{(\epsilon_{eff} + 0.3)(\frac{W}{h} + 0.264)}{(\epsilon_{eff} - 0.258)(\frac{W}{h} + 0.8)} \right)
$$
(3.8)

<span id="page-69-0"></span>

Figure 3.28: Simulated insertion and return loss of the Microstrip- CPW filter.

where  $h$  is the thikness of the substrate and  $W$  is the width of the antenna.

The antenna was connected to a microstrip feed line. The feeding line was extended inside the patch to archive the best matching. Finally, the antenna was attached to the filter, however, some optimization took place to take in account the involved discontinuity and to achieve best matching. The layout of the filter attached to the antenna is shown in Fig. [3.29.](#page-70-0) The simulated return loss of the antenna, antenna connected to the bandpass filter, and the measured return loss of the antenna with the filter together are shown in Fig. [3.30.](#page-70-0) As it is shown in the figure, the antenna has resonances at about 6.7, 7.9, and 10.1 GHz, which has been blocked by the filter, in addition to that, the antenna can be now integrated with CPW system. Good agreement has been achieved between the simulated and measured results except a small frequency shift has occurred in measured return loss, this is normally happens in the fabrication of narrow band filters and circuits especially when they have small geometry.

## 3.7 Suspended Stripline Ultra-Wideband Bandpass Filter

Suspended stripline (SSL) is considered as a multilayer structure [\[59\]](#page-139-0), [\[69\]](#page-139-0), [\[86\]](#page-141-0), since it is consisting of a substrate shielded by waveguide housing. over and below the substrate there are two layers of air. The air layers are normally having the same dimensions. Fig. [3.31](#page-71-0) shows the cross-section of the suspended stripline with the dimensions used in this section. Multi-substrates have also been proposed for such

<span id="page-70-0"></span>

Figure 3.29: Top layer CPW-microstrip filter connected to patch antenna.



Figure 3.30: Return loss of the patch antenna itself and the patch antenna with the filter.

<span id="page-71-0"></span>structures in [\[87\]](#page-141-0), and [\[88\]](#page-141-0). Due to the existence of the mount, the electromagnetic field in SSL is concentrated in the air, therefore, the effective dielectric constant is low compared to the other planar techniques, furthermore, due to same reason no radiation loss, and the dielectric loss is very low in the SSL structure. On the other



Figure 3.31: Cross-section of SSL (a) used in simulation process, (b) realized in practice.

hand the Federal Communications Commission (FCC) has released the unlicensed use of ultra-wideband (UWB: 3.1 to 10.6 GHz) wireless systems in February 2002 [\[42\]](#page-137-0). Since then, the ultra-wideband wireless communication systems with such frequency band have gained an increased interest, since they transmit higher data rates with lower transmitted power. Various filter structures have been proposed in the literature, e.g. [\[15\]](#page-135-0), [\[43\]](#page-137-0), and [\[89–92\]](#page-141-0). The combination of a lowpass filter with a high-pass filter is a classical structure for such kind of filters [\[89\]](#page-141-0), [\[90\]](#page-141-0). It occupies, however, a large area, which may increase the losses, and the group delay variation of the filter. In [\[91\]](#page-141-0), an UWB filter was built by cascading various ring filters, while, in [\[15\]](#page-135-0), and [\[43\]](#page-137-0), UWB filters were designed using multi-mode resonators. However, due to the long transmission line sections used in these structures, higher order resonances do not allow a wide stop band. An UWB filter introduced in [\[92\]](#page-141-0) was designed by employing quasi-lumped microstrip resonators built on both sides of the substrate. The fabrication of this filter, however, is difficult due to the via holes necessary to increase the stopband up to 16 GHz.

In this section, a simple ultra-wideband bandpass filter is presented, showing a great simplicity of the design concept compared to earlier known structures. The filter is realized by coupling an SSL quasi-lumped lowpass filter capacitively to the I/O ports. A very wide stopband is obtained due to the short transmission line sections used in the filter structure. The filter is built on an RT Duroid substrate with a thickness of 0.254 mm and a relative dielectric constant  $\varepsilon_r$  of 2.22. The substrate is shielded in a split-block mount with dimensions of 5 mm width and 2 mm height over and below the substrate. The substrate is suspended in the mount by extending it 0.5 mm inside the mount from both edges (Fig.3.31). The additional substrate portion within the clamping region is fully metallized to provide good connection between the mount and the substrate. This is particularly important in case of shunt connections.
Due to the small dimensions of the housing mount, the waveguide cut-off frequency is slightly above 20 GHz.

To design the ultra-wideband bandpass filter with a frequency range from 3.1 to 10.6 GHz using a lowpass filter, two steps are necessary:

We firstly design a lowpass filter with a cut-off frequency of 10.6 GHz. In general, the cut-off frequency of the lowpass filter can be adjusted by setting proper values of the lumped elements of the filter. The capacitive and inductive elements of the filter are realized by short sections of high/low-impedance transmission lines. The low impedance sections are implemented by adding a ground metallization at the backside of the substrate [\[64\]](#page-139-0), as it is descried in sec. [3.3.](#page-57-0)

Having determined all transmission line lengths the lowpass filter can be combined, however, some optimization can be done to take into account the involved discontinuities and to achieve good matching in the passband. Fig. 3.32 shows the top and backside layouts of the SSL lowpass filter. Fig. [3.33](#page-73-0) shows the simulated insertion and return loss of the filter. The filter has a cut-off frequency of 10.6 GHz, with very good matching at the passband. At about 16.5 GHz a transmission zero occurred due to the short inductive transmission line sections that allow capacitive coupling between the wide patches, and in parallel to inductances.



Figure 3.32: Top (up), and backside (down) layouts of an SSL lowpass filter.

Next, we must suppress transmission in the frequency band below 3.1 GHz. The SSL technology provides strong broadside coupling between transmission lines on the opposite sides of the substrate [\[40\]](#page-137-0), [\[24\]](#page-136-0). By overlapping a section of the original input and output lines of the lowpass filter with new input and output lines on the other side of the substrate, capacitive highpass sections [\[64\]](#page-139-0) are formed to shape the lower filter edge. Fig. [3.34](#page-73-0) shows the top and backside layouts of the filter, while Fig. [3.35](#page-73-0) shows the equivalent circuit of the structure.

The proposed filter was optimized, fabricated, clamped into the mount, and soldered to coaxial connectors fixed at the ends of the mount, see Fig. [3.36.](#page-74-0) Measurements were done using a coaxial calibration, the transitions from SSL to coaxial line

<span id="page-73-0"></span>

Figure 3.33: Simulated insertion and return loss of a SSL lowpass filter.



Figure 3.34: Top (up) and backside (down) layouts of the SSL UWB filter using a coupled lowpass filter.



Figure 3.35: Equivalent circuit of the ultra-wideband bandpass filter using a coupled lowpass filter structure.

<span id="page-74-0"></span>as well as some portion of SSL transmission line are included into the experimental results. Fig. 3.37 shows the simulated and measured return and insertion loss of the filter. As expected, the filter has a very wide stopband with a good rejection of better than 40 dB up to 25 GHz. The insertion loss of the filter in the passband is better than 0.5 dB as shown in Fig. [3.38.](#page-75-0) The group delay variation in the passband is smaller than 0.19 ns.



Figure 3.36: Photograph of the ultra-wideband bandpass filter with opened mount.



Figure 3.37: Simulated (dashed) and measured (solid) insertion and return loss of the UWB filter.

<span id="page-75-0"></span>

Figure 3.38: Simulated and measured insertion loss at the passband of the UWB filter.

# Chapter 4 Defected Ground Structures

Defected ground structures have been introduced first in [\[16\]](#page-135-0), they are known in the literature as DGS. This technique is realized by etching slots in ground plane of the microwave circuit and is namely applied for the microwave filters. This technique is used for microstrip and coplanar waveguide transmission lines. These slots are designed to achieve better performance for the microwave filters, such as increasing steepness of the cut-off slop, and to increase the stopband range of the microwave filters, moreover, compact filter can also be achieved using this technique. Many slot shapes have been introduced for microstrip technology [\[16](#page-135-0)[–23\]](#page-136-0). Increasing the stopband of microstrip lowpass filter by introducing transmission zeroes have been obtained by different slot shapes, e.g. [\[16\]](#page-135-0),[\[17\]](#page-135-0), [\[22\]](#page-136-0), and [\[34–37\]](#page-137-0). Periodic structures, e.g.[\[18\]](#page-135-0), [\[21\]](#page-135-0) and [\[93\]](#page-141-0). Even bandpass filters have been presented using this technique, e.g. [\[19\]](#page-135-0), [\[20\]](#page-135-0),[\[22\]](#page-136-0), and [\[94\]](#page-141-0). Fig [4.1](#page-77-0) shows the backside of the substrate of three different slots that have been introduced in [\[16–18\]](#page-135-0).

A simple study is done on the square head dumbbell slot with dimensions  $a=4$ mm,  $S=0.25$  mm and  $d=5$  mm etched under 50  $\Omega$  line to show how this structure behave over wide frequency band [\[16\]](#page-135-0). The insertion and return loss of the structure are shown in Fig[.4.2.](#page-77-0) It can be clearly seen that at 6.5 GHz a transmission zero occurred. Basically, the reason behind this behavior is the increase of the inductance of the transmission line and it introduces series capacitance which is in parallel to the original inductance. Thus, the equivalent circuit of a 50  $\Omega$  line over a DGS slot can be represented as a parallel resonator [\[18\]](#page-135-0), see Fig. [4.3.](#page-77-0) The current density distribution at the slot metallization is shown in Fig. [4.4.](#page-78-0) At frequencies lower than the resonant frequency of the slot, the current density is concentrated around the slot metallization as shown in Fig. [4.4a](#page-78-0). At frequencies higher than the resonant frequency of the slot (Fig[.4.4b](#page-78-0)) one can see that the current density is concentrated at the slot center. Fig. [4.5](#page-78-0) shows a representation of the wave propagating at frequencies lower and higher than the resonant frequency.

To control the resonant frequency of the DGS slot, it is required to change the dimensions of the area occupied by the slot [\[16–](#page-135-0)[23\]](#page-136-0),[\[34–37\]](#page-137-0). For example, to set the

<span id="page-77-0"></span>

Figure 4.1: Layouts of defected ground slots, (a) dumb bell structure with square head, (b) dumb bell structure with circular head, (c) U shape DGS structure.



Figure 4.2: Simulated insertion and return loss of a dumb-bell slot etched under 50-ohm transmission line.



Figure 4.3: quivalent circuit of a DGS slot etched under 50  $\Omega$  transmission line.

<span id="page-78-0"></span>

Figure 4.4: Current density distribution on the slot metallization (a) at 2.5 GHz, (b) at 9 GHz.



Figure 4.5: Representation for the wave propagating on the slot metallization (a) at frequency lower than the resonant frequency, (b) at frequency higher than the resonant frequency.

<span id="page-79-0"></span>resonant frequency of the square head dumbbell slot at low frequency it is required to increase either the dimensions of square head (a), the length of the slot (d), or both in most of the cases. Another parameter that can be set, is the spacing between the both ends of the slots [\[19\]](#page-135-0), see Fig. [4.1.](#page-77-0)

This chapter demonstrates a compact slot in form of interdigital microstrip capacitance. The resonant frequency of the line that is under-etched with this slot can be controlled by adjusting the distance between the fingers of the slot without enlarging the size of the slot. Using this slot two quasi-elliptic lowpass filters are designed. All of these filters have been design and fabricated on a RO4003c substrate that has a thickness of 0.831 and relative dielectric constant of 3.38. In addition, this chapter demonstrates a solution for the packaging problem that may occur due to the defected ground structure.

## 4.1 Interdigital DGS Slot

In this section, an interdigital DGS slot is proposed. The slot is shown in Fig. [4.6.](#page-80-0) It is etched in the ground metallization under the microstrip line. This slot has a major advantage in providing higher capacitive coupling to the line in comparison to known microstrip DGS structures. Moreover, the resonant frequency of the structure can be controlled by changing the distance between the metal fingers. The resonant frequency of the slot can also be modified by changing the number of metal fingers, so there is, in most cases, no need to enlarge the overall slot size.

The equivalent circuit of the proposed structure assuming lossless metal, illustrated in Fig. [4.7,](#page-80-0) is a combination of the interdigital capacitance equivalent circuit [\[1\]](#page-134-0) and the equivalent circuit of the DGS [\[16\]](#page-135-0). The series  $C L<sub>s</sub>$  circuit represents an equivalent circuit of the interdigital capacitance [\[1\]](#page-134-0). In the case of lossy metal, a resistance R is replaced in the equivalent circuit instead of the series inductance  $L_s$ .

Fig. [4.8](#page-80-0) shows the insertion loss of an interdigital slot in comparision with dumbbell slot. The interdigital slot has a length of 3.75 mm and a width of 4.9 mm. The slot consists of six interdigital fingers each has 3.5 mm length and 0.3 mm width. The dumb-bell slot has rectangular head with the dimensions  $a=4$  mm and  $d=5$ mm. both slots have resonance at the same frequency. this shows how much is the interdigital slot smaller than the earlier presented slot.

The current density distribution is calculated on the slot metallization at frequencies lower and higher than the resonant frequency of the slot. The current density is concentrated at the edges of the slot at frequencies lower than resonant frequency, where, at frequencies higher than the resonant frequency of the slot it is concentrated at the metallic fingers , as shown in Fig. [4.9.](#page-82-0)

Controlling the bandwidth of this slot can be done in three different ways:

1. Changing the length of the metallic fingers: The resonant frequency of the slot strongly depends on the length of the metallic fingers. Basically, by changing the

<span id="page-80-0"></span>

Figure 4.6: Backside layout of the interdigital slot.



Figure 4.7: Equivalent circuit of the interdigital DGS slot etched under 50  $\Omega$  transmission line.



Figure 4.8: Simulated insertion and return loss of the interdigital slot.

length of the fingers, the series capacitive value of the slot is changed. So increasing the length of the fingers means increasing the capacitive value of the slot and vice versa. A simple study is done on the relation between the length of the metallic fingers and the resonant frequency of the slot. The dimensions of the used slot are 3.5 mm in length and 4.9 mm in width. The spacing between metallic fingers is 0.3 mm and the number of figures is 6. Fig. [4.10](#page-82-0) shows the relation between the length of the fingers and the resonant frequency of the slot.

2. Number of fingers: It is the second parameter that is not less important than the first one. Increasing the number of metallic fingers increases the series capacitive value that the slot provides, which shifts the resonant frequency of the slot to the lower band. Decreasing the number of metallic fingers is responsible for shifting the resonance frequency of the slot to a higher frequency band. A simple parametric study was done to show the relation between the number of the fingers and the resonance frequency of the slot. The slot used in the last study is used here, the length of the used fingers is kept 3.5 mm. Fig. [4.11](#page-83-0) shows the relation between the number of the used metallic fingers and the resonant frequency of the slot. As shown in the fingers, the resonant frequency of the slot varies between 6 GHz with 6 metallic fingers and 11 GHz with one finger.

3. Spacing between fingers: As it is well known, the spacing between the interdigital fingers is an important parameter that the capacitive value of the interdigital capacitance depends on. To show that, a slot with three fingers was chosen. The length of each of the fingers was chosen to be 3.5 mm. The distance between the fingers varies between 0.2 to 1.4 mm, the other slot dimensions were kept as in the last two studies. Fig. [4.12](#page-83-0) shows the relation between the spacing between the fingers and the resonant frequency of the slot.

The inductive and the capacitive values of the slot with the transmission line above that is represented by the equivalent circuit shown in Fig. [4.7](#page-80-0) can be approximated as fowllows:

At the resonant frequency, the admittance of the equivalent circuit  $Y_{total}$  is equal to zero, where  $Y_{total}$  can be written as

$$
Y_{total} = \frac{1}{j\omega L_p} + \frac{1}{j\omega L_s + \frac{1}{j\omega C}}\tag{4.1}
$$

At the resonant frequency

$$
\frac{1}{j\omega L_p} = \frac{-1}{j\omega L_s + \frac{1}{j\omega C}}\tag{4.2}
$$

where  $L_p$ ,  $L_s$ ,  $C$  are defined in Fig. [4.7.](#page-80-0)

The transmission coefficient of the of any tow-port network is given by [\[1\]](#page-134-0)

$$
s_{21} = \frac{2Z_0}{2Z_0 + Z_{total}}
$$
\n
$$
\tag{4.3}
$$

<span id="page-82-0"></span>

Figure 4.9: Current density distribution (a) at 1 GHz, (b) 9.5 GHz.



Figure 4.10: Relation between the interdigital slot resonant frequency and the length of the metallic fingers.

<span id="page-83-0"></span>

Figure 4.11: Relation between the interdigital slot resonant frequency and the number of the metallic fingers.



Figure 4.12: Relation between the interdigital slot resonant frequency and the spacing between metallic fingers.

Where  $Z_0$  is the input impedance and  $Z_{total}$  is given as

$$
Z_{total} = \frac{j\omega L_p \left(\frac{1}{j\omega C} + j\omega L_s\right)}{\frac{1}{j\omega C} + j\omega L_s + j\omega L_p}
$$
(4.4)

at the 3dB cut-off frequency the transmission coefficient equal to  $\frac{1}{4}$  $\frac{1}{2}$  this leads to

$$
\frac{1}{\sqrt{2}} = \frac{2Z_0}{2Z_0 + \frac{j\omega L_p \left(\frac{1}{j\omega C} + j\omega L_s\right)}{\frac{1}{j\omega C} + j\omega L_s + j\omega L_p}}
$$
(4.5)

Since the major changes in the interdigital slot is on the finger lengths, the parallel inductance  $L_p$  remains unaffected. The inductive value of the inductance  $L_p$  can be simply calculated by approximating the effective dielectric constant  $\varepsilon_{eff}$  and the characteristic impedance  $Z_0$  of the transmission line with aperture under etched, which can be easily done using [\[81\]](#page-140-0). having calculated  $\varepsilon_{eff}$  and  $Z_0$ , the inductive value of of the line can be calculated using [\(3.4\)](#page-57-0).

### 4.2 Quasi Elliptic Microstrip Lowpass Filters

Quasi-elliptic filter responses are achieved by realizing equal-ripple in the passband and transmission zeros in the stopband, which leads to sharper cutoff frequency than in case of chebyshev and Butterworth filter responses, and higher rejection at the stop band. Quasi-elliptic lowpass filters are normally realized by going through two steps.

First, designing a lumped chebyshev lowpass filter, that requires the order and the cut-off frequency of the filter. Having the order, the cut-off frequency, and passband ripple, the lumped elements of the chebyshev can be simply calculated. As an example a fifth order chebyshev filter with cut-off frequency of 3 GHz and passband ripple of 0.1 dB. The normalized elements for this filter are  $g_0 = g_6 = 1, g_1 = g_5 = 1.1468$ ,  $g_2 = g_4 = 1.3712$ , and  $g_3 = 1.975$  [\[1\]](#page-134-0).  $g_0$  and  $g_6$  represent the source and load impedances, respectively, that is considered for our filters to be  $Z_0=50 \Omega$ . The proper lumped elements of the filter can be calculated by using equations [\(2.25\)](#page-35-0), and [\(2.26\)](#page-36-0). Realizing these elements in microstrip transmission line can be easily done in the same way described in sec. [3.3.](#page-57-0)

Using this way, a microstrip lowpass filter has been designed by opening apertures under the high impedance transmission line, to increase the impedances of these lines, which lead to higher inductive values for these lines that is for the classical inductive microstrip line [\[73\]](#page-140-0). Fig. [4.13](#page-86-0) shows the layout of a microstrip lowpass filter with apertures under the high impedance transmission lines [\[73\]](#page-140-0).

The response of this filter is however a chebyshev response. In other words, the filter response has no resonance at the stopband, which may introduce a transmission zero. Replacing the interdigital slot instead of the rectangular apertures will intreduce transmission zeros for the filter response. Since each slot introduces one transmission zero, thus, the number of the introduced transmission zeros is equal to the number of the replaced slots.

One transmission zero is introduced into the filter response by replacing the central aperture by the interdigital slot structure. This slot, however, shifts the cut-off frequency of the filter to a lower frequency band. To shift the cut-off frequency back, it is necessary to reduce the inductance of the narrow stripline that is located over the slot. This can be easily done by increasing the width of the strip. Fig. [4.14](#page-86-0) shows the backside layouts of the designed filter, where the top side is remained as shown in Fig. [4.13.](#page-86-0) Fig. [4.15](#page-86-0) shows the measured and simulated return and insertion loss of the filter. A transmission zero, which improves the behavior of the filter stop band, is observed at 6.32 GHz. The maximum insertion loss of the filter in the passband is better than 0.4 dB. The measured group delay variation within the passband is less than 0.275 ns.

Using two interdigital slots with different finger lengths inserted in the positions of the side apertures instead of the central one introduce two transmission zeroes. Fig. [4.16](#page-87-0) shows the top and backside layouts of the filter. Fig. [4.17](#page-87-0) shows the simulated and measured insertion and return loss of the filter. Two transmission zeros are introduced to the filter response at about 6.45 GHz and 8.6 GHz. Consequently a wide stopband was achieved. The maximum insertion loss in the passband is better than 0.5 dB. The maximum group delay variation within the passband of this filter is less than 0.26 ns.

## 4.3 Defected Ground Structure and Packaging

The defected ground structures for microstrip need much effort in packaging and in integrating it with deferent elements that are printed on one side of the substrate. Since it needs either to suspend the whole substrate by holders, such as screws , see Fig. [4.18,](#page-87-0) or drilling channel inside the carrier block of the whole system. However, the distance between the carrier block and the slot should be carefully calculated. Since it has a significant effect on the resonant frequency of the slot, which may affect the response of the filter. It may not have a large effect on the response of the lowpass filter, but the effect will be significant on the narrow bandpass filter response.

To find the relation between the dimensions of the recessed region under the DGS slot and its resonant frequency, a simple study has been done using an interdigital slot that was introduced and studied in sec. [4.1.](#page-79-0) The DGS slot has dimensions of 3.75 mm in length, 4.9 mm in width, see Fig[.4.6.](#page-80-0) The dimensions of the fingers are 3.55 mm length and 0.3 mm width, and six fingers have been used. The resonant frequency of the slot is 5.95 GHz in case of free the space used under the slot. The free space has been replaced by a metallic box with dimension of 10 mm length and 10 mm width. Fig[.4.19](#page-89-0) shows the relation between the resonant frequency of the slot

<span id="page-86-0"></span>

Figure 4.13: Top (above) and rear (below) layouts of a fifth order lowpass filter with apertures under the high-impedance transmission lines.



Figure 4.14: backside Layout of a fifth order lowpass filter with one interdigital DGS slot.



Figure 4.15: Simulated (dashed) and measured (solid) return and insertion loss of a fifth order lowpass filter with one transmission zero.

<span id="page-87-0"></span>

Figure 4.16: backside Layout of a fifth order lowpass filter with two interdigital DGS slots.



Figure 4.17: Simulated (dashed) and measured (solid) return and insertion loss of a fifth order lowpass filter with two transmission zeroes.



Figure 4.18: 3D view of suspended DGS structure.

and the height of the metallic box. As it can be clearly seen from the figure, the slot resonance changes dramatically by changing the hight the metallic box.

To reduce the packaging difficulties such as using a recessed area in the carrier block, the original ground plane of the circuit is kept fully metallized, and the interdigital slot is etched on a superstrate, which is placed on the top of the substrate. The ground plane of the substrate is connected with the metal on superstrate by via holes. Fig. [4.20](#page-89-0) shows a 3D view of the proposed structure. This structure has higher quality factor than that for the classical DGS structures, since it has narrower stopband. Fig. [4.21](#page-90-0) shows the simulated response of the proposed structure in comparison with the standard structure described sec. [4.1.](#page-79-0) The interdigital slot dimensions are defined in Fig[.4.6.](#page-80-0) The resonant frequency of proposed structure is located around 5.65 GHz which is lower than the resonant frequency of the standard DGS slot that is located at about 5.95 GHz. Moreover, the proposed structure has narrower stopband than the standard DGS.

Using this structure, a quasi-elliptic lowpass filter is designed by using two interdigital DGS slots. The filter is etched on two substrates. The dielectric constant of both substrates is 3.38, and each substrate has thickness of 0.813 mm. Since the two substrates are placed over each other, and both of them has a fully metallized ground plane, the effective dielectric constant increases, which decreases the characteristic impedance of both high and low impedance transmission lines. Thus, the high impedance line sections needed to design a lowpass filter with 3 GHz cut-off are longer than those needed to design a lowpass filter with the same cut-off frequency using the standard structure. While the opposite is correct in the case of low impedance line sections, i.e., shorter low impedance line sections are needed to design a filter for the same cut-off frequency, which compensates the increasing length of the inductive transmission line. Fig. [4.22](#page-90-0) shows the filter layout that is built on the topside of the substrate, the backside of this substrate is fully metallized. Fig. [4.22](#page-90-0) shows the metallization layout on the superstrate consisting of two interdigital slots and one aperture. The bachside of the superstrate is non-metallized. The slots that are etched on second substrate are connected with the ground plane of the first substrate by vias with diameter of 0.3 mm. After optimization the filter has been fabricated and measured. Fig. [4.24](#page-91-0) shows a photograph of the measured structure. Fig[.4.25](#page-91-0) shows measured and simulated insertion and return loss of the filter. The filter has rejection at the stopband better than 23 dB up to 8 GHz, and has insertion loss within the passband better than 0.4 dB. A good agreement between the measured and simulated results is achieved.

<span id="page-89-0"></span>

Figure 4.19: Calculated relation between the resonance frequency of the interdigital slot and the depth of the recessed region under DGS.



Figure 4.20: 3D view of the proposed structure with an interdigital slot.

<span id="page-90-0"></span>

Figure 4.21: Simulated insertion and return loss of the proposed structure (solid) in comparison with the standard DGS structure (dashed).



Figure 4.22: Top layout of a fifth order lowpass filter, the rear of the substrate is fully metallized.



Figure 4.23: 2 Metallization of the additional substrate, which contains two slots with finger lengths 3.55, and 2.45 mm, and one aperture.

<span id="page-91-0"></span>

Figure 4.24: Photograph of the fabricated lowpass filter.



Figure 4.25: Simulated (dashed) and measured (solid) insertion and return loss of a lowpass filter with the proposed DGS structure.

## Chapter 5 Dual and Triple-Mode Resonators and Filters

The classical planar filters are mostly designed using single mode resonators. In the recent years, dual-mode resonators have been increasingly used in wireless communication systems and other RF applications, since they can offer low-losses with compact size, and high selectivity. In general, the dual-mode resonator must be built in such a way that the fields are distributed symmetrically between the resonator and the ground plane. Therefore most of the known dual-mode resonator structures are built using microstrip technique. Many dual-mode resonators have been introduced using this technique. Among these resonators are the square-loop dual mode resonators, meander loop, triangular closed loop, and the hexagonal loop [\[9](#page-134-0)[–11\]](#page-135-0), and [\[95,](#page-142-0) [96\]](#page-142-0). The two resonance modes of the circular ring, square-loop, and hexagonal resonators are excited and coupled to each other by perpendicular feed line and attaching a small square patch at the corner of the resonator [\[9](#page-134-0)[–11\]](#page-135-0), Fig. [5.1](#page-93-0) shows the topologies of dual-mode resonators fed by perpendicular feeding lines. The closed loop resonators have smaller size than the patch resonators. Therefore most of the research activities nowadays are done on the loop resonators. Moreover, size reduction has been already done for such resonators by extending the loop inside the resonator [\[97\]](#page-142-0), or by connecting the original resonator by identical open-loop from the corner sides [\[98\]](#page-142-0) and [\[99\]](#page-142-0). Another class of this kind of resonators is fed by using parallel feed lines [\[95\]](#page-142-0), [\[100\]](#page-142-0) and [\[101\]](#page-142-0). Fig. [5.2](#page-93-0) shows dual mode triangular resonators as well as a meander closed loop resonator.

The main advantage of the dual-mode patches and loops is that the degenerate modes can be splitted by having a small patch attached to the resonator corner or by having a square cut (perturbation element) in one of the resonator corners. Moreover, the strength of the coupling between the degenerate modes depends on the size of the perturbation element [\[102\]](#page-142-0). The nature of the coupling between the modes depends on the shape of the perturbation element [\[3\]](#page-134-0), so by having a cut at one corner of the resonator, (see Fig. [5.3a](#page-94-0)), an inductive coupling between the modes is induced,

<span id="page-93-0"></span>

Figure 5.1: Dual-mode circular loop, patch resonator (a), square loop, patch resonator (b), square meander loop resonator (c).



Figure 5.2: Dual-mode triangular patch resonator (a), triangular closed loop (b), meander loop resonator (c).

<span id="page-94-0"></span>while attaching a small patch at the one corner will induce an capacitive coupling between the modes, (see Fig. 5.3b, and Fig. 5.3c). Furthermore, the position of the attenuation poles can also be adjusted by coupling the dual-mode resonator with feed line location not at the center of the arms of the resonator [\[103\]](#page-142-0).



Figure 5.3: (a) Dual-mode filter with inner corner cut perturbation, (b) dual-mode filter with inner corner patch perturbation, (c) dual-mode filter with outer corner patch perturbation[\[3\]](#page-134-0).

The triple-mode resonators are those resonators that provide three resonances in the passband. These resonators are efficient for bandpass filter applications. Such resonators have been introduced in the past using dielectric filled waveguide of rectangular or cylindrical shape. For most part, triple-mode operation is achieved by dielectric filled structure inside a resonant metal cavity. Then the cavity is perturbed using tuning and coupling elements such as metal rods or screws [\[104–106\]](#page-142-0). However, such structures are huge rather expensive. A triple-mode microstrip filter has been reported in [\[107\]](#page-143-0). It was realized by placing a microstrip square-loop dual mode resonator inside a cavity that provides the third resonance [\[107\]](#page-143-0). The walls of the cavity were realized by periodic metal vias that connect the top and the bottom ground plane. The fabrication of such structure may not be easily done due to the via hole needed to generate the third mode.

This chapter is divided into two parts, the first part of the chapter is introducing a simple microstrip triple-mode resonator, some parametric study is also done. The resonator is used for designing third order quasi-elliptic bandpass filters. The second part of the chapter is introducing a dual-mode suspended stirpline resonator, this resonator is used for bandpass filter design, where second and fourth order bandpass filter are designed.

## 5.1 Triple-Mode Microstrip Resonator

#### 5.1.1 Resonator Topology

A pure microstrip triple-mode resonator is introduced in this section. The resonator is realized by adding an additional path to the traditional square-loop dual-mode <span id="page-95-0"></span>resonator. The additional path is realized by a meander half wavelength strip that is connected to two opposite corners of the square-loop resonator. Fig. 5.4 shows the layout of the triple-mode and dual-mode resonators coupled by perpendicular feeding lines, and perturbed from one corner by an outer patch. Fig. 5.4a shows a second



Figure 5.4: Layout of a microstrip (a)dual-mode resonator, (b) triple-mode resonator coupled by perpendicular feeding lines and perturbed by outer patch.

order bandpass filter which consists of a square-loop dual-mode resonator [\[10\]](#page-134-0). It consists of four identical arms of length  $L$ . To couple the two modes, a small square is attached to the corner of the loop. The structure is coupled to the input and output ports by two perpendicular lines. The fundamental resonances occur when L is approximately equal to a quarter of a wavelength. The position and geometry of the corner patch determine the nature of the coupling between the two modes [\[108\]](#page-143-0).

A microstrip triple-mode resonator is created by adding an additional path to the square-loop dual-mode resonator shown in Fig. 5.4a. This path is realized by etching a meander stripline that is connected to two opposite corners of the main resonator. The length of this stripline is one half of a wavelength. Fig. 5.4b shows the layout of the resulting structure. The resonator resonates when the length of the arms is equal to one quarter of a wavelength. This additional line is again loaded by a square patch as a perturbation element with edges of length r.

#### 5.1.2 Modes and Perturbations  $p, r$

In the case of dual-mode resonators, the resonances are generated by a single even mode and one odd mode. In the case of triple-mode resonator (see Fig. 5.4b) we have two even mode and one odd mode. To justify that, we have placed a perfect magnetic wall at the symmetry plane  $(A - A')$ , i.e. the symmetry plane acts as an open circuit. Fig. [5.5](#page-96-0) shows the reflection coefficient of the un-perturbed resonator. <span id="page-96-0"></span>It is obvious that there are two resonances at 5.12 GHz, and 5.28 GHz, which gives an indication that this resonator has two even mode resonances.

For the odd mode calculation, a perfect electric wall was placed at the symmetry plane  $(A - A')$ , now the symmetry plane operates as short circuit. Fig. [5.6](#page-97-0) shows the reflection coefficient of the shorted un-perturbed resonator. From the Figure, it can be clearly seen that the resonator has a single mode resonance at 4.95 GHz.



Figure 5.5: Reflection coefficient of un-perturbed resonator using perfect magnetic wall at the symmetry plane.

For un-perturbed resonator coupled to two perpendicular feeding lines, the filter response shows two un-splitted mode resonances, while the third mode resonance is located on a different frequency band, furthermore, the filter is not well matched by using un-perturbed resonator. Fig. [5.7](#page-97-0) shows the reflection coefficient of the un-perturbed resonator fed by two perpendicular feeding lines.

In order to split the modes, two square patches are attached to two corners of the triple-mode resonator, (see [5.4b](#page-95-0)), the dimensions of the resonator chosen for the analysis are as the following, the length of each arm of the resonator  $L = 10$  mm, and the width of the arm strips are  $d = 0.3$  mm. Fig. [5.8](#page-98-0) shows the dependence of mode resonances on the perturbation elements on  $p$ , where  $p$  is the length of the square patch that is located at the outer side of the resonator, while keeping  $r = 0$ mm, where  $r$  is the length of the inner square patch. From the figure it is clearly seen that the resonance mode  $f_{03}$  is not affected by the perturbation element p, while the modes  $f_{01}$ ,  $f_{02}$  start splitting when the dimension  $p > 0.2$  mm.

Keeping the perturbation element un-presented  $(p = 0)$ , and increasing the dimensions of the inner perturbation element  $r$ , see Fig[.5.4b](#page-95-0), the third-mode resonant frequency  $f_{03}$  decreases, while the other two modes remain un-splitted. When the

<span id="page-97-0"></span>

Figure 5.6: Reflection coefficient of un-perturbed resonator using perfect electric wall at the symmetry plane.



Figure 5.7: Reflection coefficient of un-perturbed resonator fed by two perpendicular feeding lines.

<span id="page-98-0"></span>

Figure 5.8: Relation between the size of the perturbation element  $p$  and the triplemode resonance frequencies, perturbation r is not presented  $(r=0)$ .

dimension  $r > 0.7$  mm, all the modes share the same resonant frequency. Fig. 5.9 shows the relation between the resonant frequencies and the size of the perturbation element r.

#### 5.1.3 Triple-Mode Resonator and Filter Realization

Based on the above information, a third order bandpass filter has been designed. The dimensions of the filter were chosen as follows,  $L = 10$  mm,  $d = 0.3$  mm,  $p = 0.9$  mm,  $r = 0.2$  mm, the spacing between the resonator and the stubs that are connected to the feed lines is 0.2 mm. The filter has bandwidth of 0.3 GHz and centre frequency about 5.06 GHz. The coupling coefficient between the modes should be computed according to the theory of the coupled asynchronously tuned resonators as [\[2\]](#page-134-0)

$$
k_{nm} = \left(\frac{f_{sm}}{f_{sn}} + \frac{f_{sn}}{f_{sm}}\right) \sqrt{\left(\frac{f_{om}^2 - f_{0n}^2}{f_{om}^2 + f_{0n}^2}\right)^2 - \left(\frac{f_{sm}^2 - f_{sn}^2}{f_{sm}^2 + f_{sn}^2}\right)^2}
$$
(5.1)

where  $f_{sm}$  and  $f_{sn}$  are the self-resonant frequencies of the resonator and  $f_{0m}$ ,  $f_{0n}$  are the mode splitting frequencies. From the simulated results, we denote that the selfresonant frequencies are equal to the mode splitting frequencies. That leads to  $k=0$ . Therefore, the filter has a transversal coupling scheme [\[109\]](#page-143-0), This means that each resonator is coupled with the source and the load in addition to the coupling between the source and the load, Fig. [5.10](#page-99-0) shows the transversal coupling scheme of the our third order filter. The used coupling matrix for this analysis is  $(N + 2) \times (N + 2)$ , which supports analysis of fully canonical filtering function, i.e. the number of the

<span id="page-99-0"></span>

Figure 5.9: Relation between the size of the perturbation element  $r$  and the triplemode resonance frequencies, perturbation  $p$  is not presented  $(p=0)$ .

finite transmission zeros equal to the order of the filter.



Figure 5.10: Coupling and routing scheme of the triple-mode filter.

The filtering function that characterizes the filter can be written as a rational function

$$
F(\omega') = \frac{P(\omega')}{D(\omega')}
$$
\n(5.2)

Where  $\omega'$  is the low-pass prototype frequency related to the actual frequency  $\omega$  by

$$
\omega' = \frac{\omega_0}{\Delta \omega} \left( \frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \right)
$$
\n(5.3)

The polynomial  $P(\omega')$  is computed from a recursion method introduced in [\[110\]](#page-143-0) which is given as

$$
P_{N+1}(\omega) = -P_{N-1}(\omega') \left(1 - \frac{\omega'}{\omega'_N}\right)^2 \frac{\left(1 - \frac{1}{\omega_{N+1}^2}\right)^{0.5}}{\left(1 - \frac{1}{\omega'_N}\right)^{0.5}}
$$

$$
+ P_N(\omega') \left[\omega' - \frac{1}{\omega'_{N+1}} + \left(\omega' - \frac{1}{\omega'_N}\right) \frac{\left(1 - \frac{1}{\omega_{N+1}^2}\right)^{0.5}}{\left(1 - \frac{1}{\omega'_N}\right)^{0.5}}\right]
$$
(5.4)

where  $\omega'_{N}$  is the position of the pre-defined attenuation pole,  $P_{0}(\omega') = 1$  and  $P_{1}(\omega') =$  $\omega'-\frac{1}{\omega'}$  $\frac{1}{\omega'_1}.$ 

The Polynomial  $D(\omega')$  can be given as

$$
D(\omega') = \prod_{N=1}^{K} \left( 1 - \left( \frac{\omega'}{\omega'_N} \right) \right),\tag{5.5}
$$

where  $\omega_N$  represents the  $N^{th}$  attenuation pole. The transmission coefficient can be expressed as

$$
|S_{21}(\omega')|^2 = \frac{1}{1 + \epsilon^2 F^2(\omega')},\tag{5.6}
$$

where the parameter  $\epsilon$  is a constant related to the passband return loss RL, it is expressed by the following formula

$$
\epsilon = \left[10^{\frac{RL}{10}} - 1\right]^{-0.5} \tag{5.7}
$$

The loop currents through the filter resonators can be grouped in a vector I and given by the following matrix form [\[111\]](#page-143-0)

$$
[-jR + \omega lW + M]I = AI = -jE,
$$
\n(5.8)

where R is an  $(N+2) \times (N+2)$  matrix with zeros entries except  $R_{1,1}=R_{N+2,N+2}=1$ , W is an  $(N + 2) \times (N + 2)$  diagonal matrix whose main diagonal elements are ones except  $W_{1,1}=W_{N+2,+2}=0$ , M is the normalized coupling matrix, and  $E = \begin{bmatrix} 1, 0, ..., 0 \end{bmatrix}$ is the excitation vector. The transmission and reflection coefficients  $S_{11}$  and  $S_{21}$  are given by

$$
S_{12} = -2j[A^{-1}]_{N+2,1} \tag{5.9}
$$

$$
S_{11} = 1 + 2j[A^{-1}]_{1,1} \tag{5.10}
$$

The synthesis problem can be formulated as follows. Looking for the suitable coupling matrix  $M$  that minimizes a certain cost function  $C$ , so that the entries of the optimization function are the non-zero elements of the coupling matrix with initial guess. The cost function to be minimized can be expressed as

$$
C = \sum_{i=1}^{K} |S_{11}(\omega'_{p_i})|^2 + \sum_{i=1}^{H} |S_{12}(\omega'_{tz_i})|^2 + \left(|S_{11}(\omega' = \mp 1)| - \frac{\epsilon}{\sqrt{1 + \epsilon^2}}\right)^2 \tag{5.11}
$$

where  $p_i$ ,  $tz_i$ , and H are the positions of the poles (roots of  $P(\omega')$ ), the positions of the attenuation poles, and the number of the attenuation poles, respectively. The flow chart shown in Fig. 5.11 explains the optimization procedure used to synthesize the filter response. The scheme starts by an initial guess of the coupling coefficients, then calculates the matrices [A] and  $[A]^{-1}$  at the roots of the polynomials  $P(\omega')$  and  $P(\omega t)$ . After that the const function is calculated and checked whether it satisfies a predefined value, if not the scheme changes the initial values and calculates C again until achieving the satisfied value.



Figure 5.11: flow chart of the used optimization method.

Due to the symmetry of the structure its modes exhibit either a magnetic wall or an electric wall along the main diagonal. It is important to keep in mind that these modes are determined with reference planes placed right at the coupling stubs at the input and output. Under the lossless assumption, these modes are not coupled to each other but are all coupled to the input and the output. Higher order modes, including surface modes, contribute to a small direct coupling between the input and the output. A narrowband equivalent circuit based on this coupling scheme is shown in Fig. [5.10,](#page-99-0)which is a transversal coupling matrix [\[105\]](#page-142-0). The narrowband response of this filter is, therefore, described by a coupling matrix of the form

$$
M = \begin{pmatrix} 0 & M_{s1} & M_{s2} & M_{s3} & M_{sl} \\ M_{s1} & M_{11} & 0 & 0 & M_{l1} \\ M_{s2} & 0 & M_{22} & 0 & M_{l2} \\ M_{s3} & 0 & 0 & M_{33} & M_{l3} \\ M_{sl} & M_{l1} & M_{l2} & M_{l3} & 0 \end{pmatrix}
$$
 (5.12)

Since there are two even modes and one odd mode in this third order structure with a symmetry plane along the main diagonal. At the coupling matrix level, this implies that one of the coupling coefficients to the ports is negative. This is taken as the third resonance leading to the choice

$$
M_{s1} = M_{l1}, \quad M_{s2} = M_{l2}, \quad M_{s3} = -M_{l3} \tag{5.13}
$$

The filter response is compared with a third order chebyshev response. However, a disagreement between EM and the synthesized filter indicates that complex attenuation poles exist at the upper stopband. Therefore a filter has been synthesized as transversal, assuming two attenuation poles on the real axis of the s-plane addition to one transmission zero located at the lower stopband, which is laying on the imaginary access of the s-plane. For given specifications, the entries of the coupling matrix can be extracted analytically by following the presentation in [\[109\]](#page-143-0). For example, for a third order filter with an in-band return loss of 20 dB, one attenuation pole at  $s=6.471$  and a pair of complex transmission zeros at  $s=\pm 2.25$ , we get the following coupling matrix

$$
M = \left(\begin{array}{cccccc} 0.0000 & 0.6441 & -0.5648 & 0.7152 & -0.0307 \\ 0.64411 & -1.4992 & 0.0000 & 0.0000 & 0.64411 \\ -0.5648 & 0.0000 & 1.4756 & 0.0000 & -0.5648 \\ 0.7152 & 0.0000 & 0.0000 & 0.1061 & -0.7152 \\ -0.0307 & 0.7152 & -0.5648 & -0.7152 & 0.0000 \end{array}\right)
$$

A filter was designed to implement this coupling matrix. Its response is shown in Fig. [5.12](#page-103-0) along with that of this coupling matrix. Good agreement is achieved between The EM simulation and the coupling matrix synthesized results .

Changes to the dimensions of perturbation elements  $p$  and  $r$  lead to changes in the positions of the transmission zeros. These zeros can even be migrated in the complex plane from the real axis to the imaginary axis, and vice versa [\[3\]](#page-134-0), and [\[108\]](#page-143-0). The positions of the transmission zeros can also be controlled by adjusting the electrical length between the I/O feeding lines [\[103\]](#page-142-0), [\[112\]](#page-143-0). Fig. [5.13](#page-104-0) shows the insertion loss of the filter with different feed line positions  $a$ , where  $a$  is the distance between the feeding lines and the centre of the resonator arms, as shown in Fig. [5.4b](#page-95-0). As can be clearly seen, with the I/O feeding lines connected at the centre of the feeding stub  $a = 0$ , the transmission zeros at the higher stopband disappear (i.e., the transmission zeros are located on the real axis of the complex s-plane), and the attenuation pole that is in the lower stopband is located at  $s = -6.346$ . By increasing a, see Fig. [5.4b](#page-95-0),

<span id="page-103-0"></span>

Figure 5.12: EM simulation (solid) synthesized (dashed) reflection and transmission coefficients of a triple-mode bandpass filter.

the positions of the transmission zeros are moved, and are possibly transferred on to the imaginary axis of the complex s-plane.

A triple-mode filter with the feed line located at  $a=1.35$  mm was designed as shown in the previous section. It has a centre frequency of 5.06 GHz, a bandwidth of 220 MHz, and three attenuation poles at  $s = -1.497j$ , 3.317j, and 7.86j, respectively. The resulting coupling matrix of the coupling scheme shown in Fig. [5.10](#page-99-0) is

$$
M = \left(\begin{array}{cccc} 0.0000 & 0.4820 & -0.3377 & -0.7599 & -0.0235 \\ 0.4820 & -1.2827 & 0.0000 & 0.0000 & 0.4820 \\ -0.3377 & 0.0000 & 1.2083 & 0.0000 & -0.3377 \\ -0.7599 & 0.0000 & 0.0000 & 0.2281 & 0.7599 \\ -0.0235 & 0.3377 & -0.3377 & 0.7599 & 0.0000 \end{array}\right)
$$

The filter response based on this coupling matrix and compared with the EM simulation is shown in Fig[.5.14.](#page-104-0) Good agreement between the two results is achieved, except at the stopbands, as the coupling matrix can only be applied in a narrowband range.

#### 5.1.4 Broadband Equivalent Circuit

The coupling matrix describes the filter behavior properly only in the close vicinity of the passband, see Fig. [5.14.](#page-104-0) Consequently, some design tools working in a wider frequency band are required. For this purpose, an equivalent circuit has been found as a very effective way to analyze the filter. This circuit is shown in Fig. [5.15.](#page-105-0) It is simply derived from the filter layout in Fig. [5.4b](#page-95-0). This equivalent circuit is based on

<span id="page-104-0"></span>

Figure 5.13: Transmission coefficient of a triple-mode bandpass filter with various a values.



Figure 5.14: EM simulation (solid) synthesized (dashed) reflection and transmission coefficients of triple-mode bandpass filter with three transmission zeros.

<span id="page-105-0"></span>the representation of the microstrip line. The effective dielectric constant  $\varepsilon_{eff}$ , and the characteristic impedance of this line is well defined in [\(2.84\)](#page-46-0), [\(2.85\)](#page-46-0).



Figure 5.15: Broadband equivalent circuit of the triple- mode mictrostrip filter. The inset shows the circuit used to determine  $C_s$ .

Having calculated  $\varepsilon_{eff}$  and  $Z_c$ , the electrical length of each transmission line can easily be calculated by

$$
\Theta = L\beta \tag{5.14}
$$

where L is the physical transmission line length and  $\beta$  is the propagation constant, which is defined as

$$
\beta = \frac{2\pi}{\lambda_g} \tag{5.15}
$$

where

$$
\lambda_g = \frac{\lambda}{\sqrt{\varepsilon_{eff}}} \tag{5.16}
$$

For our filter, which has dimensions  $L=10$  mm and  $L_x = 3.4$  mm, where  $L_x =$  $L-a$ , we obtained  $\theta = 90^{\circ}$ , 29<sup>o</sup>, respectively. The capacitances of the perturbation elements can be approximated as in [\[3\]](#page-134-0)

$$
C_i = \sqrt{2}C_0, \quad i = p, r \tag{5.17}
$$

where

$$
C_0 = \varepsilon_0 \varepsilon_r \frac{A_i}{h}, \quad i = p, r \tag{5.18}
$$

where  $A_i$  is the area of the perturbation elements, h is the thickness of the substrate,  $\varepsilon_r$  is the relative dielectric constant of the substrate, and  $\varepsilon_r$  is the free-space dielectric constant.

Capacitance  $C<sub>S</sub>$  that is between the resonator and the stubs connected to the feeding lines was determind by calculating the capacitance between the feeding line terminated by the stub and its mirror image, as shown in the inset of Fig. [5.15.](#page-105-0)

Capacitance  $C_{Ports}$  representing the direct coupling between the filter ports cannot be simply and directly determined. Fig 5.16 shows the transmission characteristics of the equivalent circuit from Fig. [5.15](#page-105-0) calculated for selected values of  $C_{Ports}$ , this calculation has been done using a circuit simulator [\[113\]](#page-143-0). This capacitance is finally determined by fitting these results to the characteristic obtained by the EM simulation. The final fit using  $C_{Ports} = 0.01 \text{ pF}$  is shown in Fig. [5.17.](#page-107-0)



Figure 5.16: Transmission coefficient of the Broad-band equivalent circuit for different values of  $C_{Ports}$ .

#### 5.1.5 Experimental Results

The two triple-mode filters were designed using the proposed resonator. The first filter has dimensions of  $L = 10$  mm,  $d = 0.3$  mm,  $p = 0.9$  mm,  $r = 0.2$  mm, and the spacing between the resonator and the stubs connected to the feed lines is  $w = 0.2$ mm. This filter has one transmission zeros in its lower stop band and two complex attenuation pole. A photograph of the fabricated structure is shown in Fig[.5.18.](#page-107-0) The simulated and measured return and insertion loss of the filter are shown in Fig[.5.19.](#page-108-0) There is good agreement between the two results, apart from a small shift at the lower cut-off frequency. The maximum return loss at the pass band is about 11 dB, which can be attributed to fabrication errors. The insertion loss at the passband is better than 2.9 dB; this relatively high magnitude of the insertion loss corresponds

<span id="page-107-0"></span>

Figure 5.17: EM simulation (solid) and equivalent circuit simulation (dashed) when  $C_{Ports} = 0.01 \text{ pF}.$ 

to the high return loss at the passband. The group delay variation in the passband is smaller than 0.51 ns.



Figure 5.18: Photograph of a third order bandpass filter using the proposed triplemode resonator.

The second filter is designed to have the same resonator dimensions; the only change concerns the locations of the feeding lines. The feeding lines are located offcenter at a=1.35 mm, see Fig. [5.4b](#page-95-0). The filter has three transmission zeros, one in the lower stopband, and two in its upper stopband. Fig. [5.20](#page-108-0) shows the simulated and measured insertion and return loss of the filter. The two transmission zeros in the upper stopband considerably improve the filter behavior in this stopband, in comparison with the characteristics of the first filter version. The in-band insertion loss is better than 2.3 dB. The group delay variation in the passband is smaller than 1.5 ns.


Figure 5.19: Simulated(dashed) and measured (solid) insertion and return loss of trip-mode bandpass filter with one transmission zero.



Figure 5.20: Simulated(dashed) and measured (solid) insertion and return loss of trip-mode bandpass filter with three transmission zeroes .

### <span id="page-109-0"></span>5.2 Dual-Mode Suspended Stripline Filters

Dual-mode resonators have not been introduced for suspended stripline technique with their classical structure. Since they require increasing the cross section of suspended stripline, that will increase the size of the overall filter structure. Due to the large cross-section, the waveguide mode may not allow a wide stopband. Up to now, the filters designed using suspended stripline are done using either the folded transmission lines, or by using quasi-lumped elements.

In this section a dual-mode suspended stripline resonator is introduced. The resonator is realized by combining quasi-lumped suspended stripline parallel resonator with open-loop resonator. These two resonators were chosen to be combined with each other because they have nearly the same size at the corresponding resonance frequency. A second order, and two fourth order filters are realized using this resonator. The realized filters are very compact compared to those realized by quasi-lumped resonators.

#### 5.2.1 Quasi-Lumped Parallel Resonator

The parallel resonator has been introduced first in [\[114\]](#page-143-0). The resonator consists of a narrow strip connected to the side wall of the metal housing and patch at the other end, see Fig. [5.21a](#page-110-0). The narrow stripline represents a shunt inductance, while the coupling between the patch and the walls of the mount represents a shunt capacitance, see Fig. [5.21b](#page-110-0). The resonance frequency of the resonator can be controlled either by changing the length of the narrow stripline, or by changing its width. The other parameter that plays a role in controlling the resonance frequency of the resonator is the spacing between the patch and the housing mount. Locating the narrow stripline on the same side induces an additional inductive coupling between the two resonators, which in turn, introduces a transmission zero to the filter response [\[115\]](#page-143-0). The position of the transmission zero can be easily adjusted by increasing or decreasing the distance between these strips. Different filter types, broadband bandpass filters, wltra-wideband bandpass filters, and high-pass filters have been designed using this resonator. [\[24\]](#page-136-0), [\[90\]](#page-141-0), and [\[115\]](#page-143-0).

#### 5.2.2 Open-Loop Resonator

Open-loop resonator also known in the literature as split-ring resonator. This resonator resonates when the length of the resonator corresponds to  $\lambda/2$  [\[2\]](#page-134-0), [\[4\]](#page-134-0), and [\[116–118\]](#page-143-0). The open end of resonator provides a capacitive coupling in parallel to the main path that provides a transmission zero at the higher stopband [\[116\]](#page-143-0). Due to the fact that the electric field at the open sides of the open-loop resonator is maximum at the resonance frequency of the resonator, and the magnetic field is maximum at the center of the resonator ; the coupling nature between two open-loop depends on the

<span id="page-110-0"></span>

Figure 5.21: (a) Layout of suspended stripline quasi-lumped resonator, (b) equivalent circuit of the suspended stripline resonator .

neighboring sides [\[4\]](#page-134-0). Thus, by having the resonators coupled from the open-ends, capacitive coupling is generated, see Fig. 5.22a, while having the resonators coupled from the opposite sides, an inductive coupling is generated, see Fig. 5.22b. To generate a mixed coupling between the resonators, the resonators can be built keeping open ends on one side, or by keeping the open ends antipodal, see Fig. 5.22c and Fig. 5.22d. Size reduction has been already done by extending the loop in idle area inside the resonator itself and by increasing the capacitive coupling between the open ends [\[8\]](#page-134-0). The open-loop resonator can be easily realized using suspended stripline technique, see Fig[.5.23](#page-111-0)



Figure 5.22: Coupling structures for microstrip open-loop resonator (a) capacitive coupling structure, (b) inductive coupling stricture, (c) mixed coupling structure, (d) mixed coupling structure [\[4\]](#page-134-0).

#### 5.2.3 Resonators Combination

Combining both quasi-lumped resonator with open-loop, an SSL dual mode resonator can be realized. The new resonator is realized by adding a narrow stripline to the open-loop resonator, as shown in Fig. [5.24.](#page-112-0) Using this configuration, the quasilumped resonance in addition to the open-loop resonant mode is generated. Fig [5.25](#page-112-0)

<span id="page-111-0"></span>

Figure 5.23: Suspended stripline open-loop resonator.

shows the return loss of the new resonator capacitively coupled to the feeding lines in comparison with return loss of the open-loop resonator. Controlling the resonant frequencies of the resonators must be done in such a way that it does not affect the size or the shape of the resonator, because this will affect both resonances, which makes it difficult to adjust the center frequency of the filter, and increases the difficulties in achieving a good matching at the passband of the filter.

The parameters that control the resonance frequencies are:

- 1. The width of the narrow stripline  $w$ , see Fig. [5.24,](#page-112-0) which affects only the quasi-lumped resonance without main change of the open-loop resonance, so by increasing  $w$ , the inductive value of the stripline is decreased, that will shift the quasi-lumped resonance to a higher frequency band, and vice versa.
- 2. The other parameters that mainly affect the open-loop resonance are, the spacing between the open ends of the resonator s, and the width of the open ends  $x$ , see Fig. [5.24.](#page-112-0) Decreasing s decreases the capacitive coupling between the open ends of the resonator, which shifts the open-loop mode to a higher frequency, and vise versa. On the other hand, increasing  $x$  increases the capacitive value between the open ends which shifts the open-loop mode to lower frequency band.

An easy way to design a filter using this resonator is to design two filters on the same frequency band. The first one by quasi-lumped resonator, and the second by open-loop. The size of the two resonators must be kept the same, in other words, the size of the patch must be equal to the outer frame of the open-loop resonator.

Coupling between the two modes of the dual-mode resonator is the next step. For this resonator the modes can be coupled by two ways. The first one is realized by increasing external coupling, this can be easily done using suspended stripline, since overlapping between the metallization on both sides of the substrate is allowed. A second order bandpass filter has been designed by using one resonator on the backside of the substrate coupled tightly with feeding lines that built on the topside of the substrate, the cross section of the transmission line used for this filter is shown in

<span id="page-112-0"></span>

Figure 5.24: Suspended stripline open-loop resonator.



Figure 5.25: Simulated return loss of the dual-mode resonator (dashed) in comparison with the return loss of the open-loop (solid).

Fig[.3.31.](#page-71-0) Fig. 5.26 shows a 3D view of the filter, while Fig. 5.27 shows the simulated insertion and return loss of the filter.



Figure 5.26: 3D view of a second order bandpass filter using SSL dual-mode resonator intensively coupled with the feeding lines.



Figure 5.27: Simulated insertion and return loss of a second order bandpass filter using SSL dual-mode resonator intensively coupled with the feeding lines.

The second parameter that increases the coupling between the resonator modes is the position of the narrow stripline. Having asymmetry of the inductive strip, the modes of the resonators will be coupled and matched better than implementing the inductive strip at the center of the resonator. This principle is used to the design of a fourth order bandpass filter. Two coupled SSL dual-mode resonators have been implemented on the backside of the substrate. Each of these resonators is coupled to the neighboring port, which is implemented on the topside of the substrate. The parallel inductive strips are located on different sides of the substrate to avoid any inductive coupling between both resonators (see [\[24\]](#page-136-0), [\[115\]](#page-143-0)). Fig. 5.28 shows a 3D view of the fourth order bandpass filter structure, the filter has a length of 7.25 mm, which is much smaller than the forth order that is designed using quasi-lumped elements, see [\[24\]](#page-136-0). Fig. 5.29 shows the simulated return and insertion losses of the filter. The four return-loss poles can be observed clearly. In addition, a transmission zero occurs at about 14 GHz. This occurs due to the slot that is in parallel to the narrow stripline at the other side of the resonator. The filter has a bandwidth of about 2 GHz, and a center frequency of 10.8 GHz.



Figure 5.28: 3D view of forth order bandpass filter using two dual-mode resonators.



Figure 5.29: Simulated insertion and return loss of a fourth order bandpass filter using SSL dual-mode resonator.

As it has been already demonstrated in [\[24\]](#page-136-0), [\[115\]](#page-143-0), locating the parallel inductive strips of two resonators on the same side of the substrate, introduces an inductive coupling in parallel to the original capacitive coupling. This causes an additional transmission zero. The same principle has been transferred to our design. An additional transmission zero has been introduced below the passband. The transmission zero which was introduced in the last structure is splitted now into two zeroes. Fig. 5.30 shows the simulated filter structure, while Fig. 5.31 shows a photograph of the measured structure, the filter is 6.45 mm in length, Fig[.5.32s](#page-116-0)hows the simulated and the measured return and insertion losses of this filter. The general behavior of the insertion loss is well met. A slight frequency shift is due to the increased resonator inductance caused by a groove in the mount clamping the substrate. The maximum return loss is about 9 dB. This is due to fabrication errors, combined with the relatively high sensitivity of this type of filters. The measured insertion loss is smaller than 1.8 dB where most of this is caused by the problem in the return loss.



Figure 5.30: 3D sketch of a fourth order SSL bandpass filter using two dual-mode resonators with parallel inductive strips on one side.



Figure 5.31: Photograph of fourth order bandpass filter structure.

<span id="page-116-0"></span>

Figure 5.32: Measured (solid) and simulated (dashed) return and insertion losses of the fourth order bandpass filter with additional transmission zero.

# Chapter 6 Dual-Band Bandpass Filters Using Dual-Mode Resonator

Dual-band filters have gained much interest in the recent years. Deferent filter approaches have been introduced during the last ten years to meet the demand of the modern wireless communication systems e.g., [\[46–52\]](#page-138-0) and [\[119–125\]](#page-144-0). The classical dual-band bandpass filter approach has been achieved by connecting two individual bandpass filters with each other in parallel. However, such approach needs additional matching network that increases the size of the overall filter structure [\[46\]](#page-138-0), [\[123\]](#page-144-0) and [\[124\]](#page-144-0). Another approach using the dual-band stubs [\[47\]](#page-138-0), however, due to the inductive coupling between these stubs, the filter has also transmission at low frequency, and attenuating lowpass band has not been reported so far. In [\[52\]](#page-138-0) and [\[119–121\]](#page-144-0), dualband filter structures have been introduced using stepped impedance resonator (SIR), but due to the long transmission line sections used in this class of filters, the filter response does not have wide upper stopband. In addition, high losses are introduced to the filter response. Dual-band filter has been also achieved by using dual-mode resonators. In [\[125\]](#page-144-0) a CPW dual-band filter has been designed by using two dualmode resonators each of the resonators resonates at different frequency band. The resonators have been built using back-to-back microstrip ring resonator, this filter has a main advantage, which is the center frequency of each band is independent on the other. Moreover, the filter has been modified by building the smaller resonator inside the bigger one, by this configuration the filter has smaller volume. However, realizing this structure in microstrip technology requires to have cuts at the feeding line sides and to let the feeding lines pass the dual-mode resonators under air bridges [\[122\]](#page-144-0). By this configuration the coupling between the resonators and the feed lines can be easily controlled, however, this will increase the fabrication cost and the fabrication tolerance.

In this chapter, two simple, low-loss dual-band bandpass filters using the dualmode resonators are proposed. The first filter is a microstrip one, and it is design by introducing transmission zeros inside the passband of broadband bandpass filter using dual-mode resonator. The second one is a suspended stripline filter, it is realized by splitting the modes of the dual-mode resonator into two bands.

### 6.1 Dual-Band Microstrip Filter

#### 6.1.1 Filter Topology

Broadband bandpass filter using square loop is shown in Fig. 6.1. It is basically a form of multiple-mode resonator, which is coupled capacitively with input/output ports [11]-[13]. The resonator consists of a square-loop dual-mode resonator with a length of  $l<sub>D</sub>$  instead of the low-impedance transmission line section, connected from both sides high transmission lines with the length of  $l_T$ . These transmission lines are coupled from the other side capacitively to two transmission lines having the same length and connected to the input/output ports from the other side. Fig. 6.2 shows the insertion loss of the filter.



Figure 6.1: Layout of the broadband bandpass filter using multiple-mode resonator with a square-loop dual-mode resonator at the center of the filter.



Figure 6.2: Insertion loss of the broadband bandpass filter with  $l_D = l_T = 10$  mm.

Rotating one of the high impedance transmission line sections with one of the feeding lines  $90^{\circ}$ , as shown in Fig. [6.3,](#page-120-0) two transmission zeros are introduced in the <span id="page-120-0"></span>passband of the broadband bandpass filter. These two transmission zeros are splitting the passband of the filter into two passbands. Fig. 6.4 shows the insertion loss of the dual-band bandpass filter using dual-mode resonator. In case  $l_D$  is equal to  $l_T$  then the bandwidth of both bands is equal, since the transmission zeros are introduced in the middle of the passband of the original broadband filter.



Figure 6.3: Layout of the dual-band bandpass filter using multiple-mode resonator with a square-loop dual-mode resonator at the center of the filter.



Figure 6.4: Insertion loss on dual-band bandpass filter with dimensions  $l_D = l_T = 10$ mm, the width of all transmission lines is 0.3 mm.

#### 6.1.2 Center Frequency and Bandwidth Control

The center frequencies of the filter can be easily shifted by changing the dimensions of both transmission lines length  $l_T$  and the length of dual-mode resonator arms  $l_D$  with the same value, see Fig. [6.3.](#page-120-0) Fig. 6.5 demonstrates the relation of the insertion loss of the filter by choosing  $l_D = l_T = 5$  mm, 10 mm, and 15 mm, respectively, while keeping the dimensions of the perturbation patch at  $p=0.5$  mm, and the width of the attached transmission line and the arms of square-loop resonator at 0.3 mm fixed.



Figure 6.5: Simulated return loss of a dual-band bandpass filter with  $l_D = l_T = 5$ , 10, 15 mm.

One of the main advantages of this filter is that the bandwidths of both bands can be controlled by different parameters:

1. Bandwidth Control by Adjusting the Length of the Attached Transmission Lines  $l_T$ :

Changing the length of the attached transmission lines only affects the outer cut-off frequencies of the filter, while the transmission zeros remain unaffected, which leads to major effect on bandwidth of both bands. So by choosing  $l_T$ longer than the  $l<sub>D</sub>$ , the bandwidth of the lower band increases and that of the higher band decreases. The opposite applies too, choosing the length of the attached transmission line  $l_T$  smaller than the length of arms of the dual-mode resonator decreases the bandwidth of the lower band and increases that of the higher band. This basically occurs due the transmission zeroes that remain fixed. This can be clearly seen in Fig. [6.6,](#page-122-0) which shows the simulated insertion loss of the filter for different transmission lines lengths  $l_T$  and keeping  $l_D = 10$ mm.

2. Bandwidth Control by Adjusting the Length of the Square-Loop Resonator Arms  $l_D$ :

<span id="page-122-0"></span>

Figure 6.6: Simulated insertion loss of the dual-band bandpass filter with different  $l_T$ values, with  $l_D = 10$  mmm.



Figure 6.7: Simulated insertion loss of the dual-band bandpass filter with different  $l_D$  values with  $l_T = 10$  mm.



Figure 6.8: Simulated insertion loss of the dual-band bandpass filter with different p values, with  $l_p = l_T = 10$  mm.

Changing the length of the dual-mode resonator arms will basically influences the position of the transmission zeroes. This in turn affects the bandwidth of the both bands. Increasing the length  $l<sub>D</sub>$ , shifts the transmission zeroes to a lower band, which leads to having a narrower bandwidth of the lower band and wider bandwidth of the higher band. Shortening the arms shifts the transmission zeroes to a higher frequency band, which increases the bandwidth of the lower band and decreases that of the higher band. Fig. [6.7](#page-122-0) shows the corresponding insertion loss.

3. Splitting the transmission zeroes can be easily done by increasing the dimensions of the square patch  $p$  attached to the inner side of the square-loop dual-mode resonator. Fig. 6.8 shows the effect of the square patch dimensions and the simulated insertion loss of the dual-band bandpass filter. It is clear from Fig.6.8 that the longer the patch dimensions  $p$ , the more the transmission zeroes are splitted, which affects the sharpness of inner cut-off frequencies slops of both bands, so by increasing the inner cut-off slops become sharper, that may affect the bandwidth.

#### 6.1.3 Experimental Results

A dual-band bandpass filter has been designed, fabricated and measured on RO4003c substrate.It has a thickness of 0.813 mm and a relative dielectric constant of 3.38. The width of the attached transmission line and the arms of the dual-mode resonator were chosen to be each 0.3 mm. The lengths  $l_T= l_D = 10$  mm, and the dimension  $p =$ 0.5 mm. Fig. [6.9](#page-124-0) shows the simulated and measured return and insertion loss of the <span id="page-124-0"></span>filter. The filter has center frequencies of 3.45 GHz, and 6.65 GHz, and bandwidths of 0.5 GHz and 0.55 GHz, respectively. The insertion loss within the pass bands is better than 0. 7 dB for the lower band, and is better than 1.2 dB for the higher band. Good agreement between the measured and the simulated results is obtained.



Figure 6.9: Simulated and measured return and insertion loss of a dual-band bandpass filter with dimensions  $l_D = l_T = 10$  mm.

# 6.2 Dual-Band Suspended Stripline Filters Using Dual-Mode Resonator

In this section the suspended stripline dual-mode resonator that has been introduced in sec. [5.2](#page-109-0) is used for dual-band filter realization. The modes of the resonator are splitted into two frequency bands. As it has been mentioned, this resonator generates two modes, the first one is quasi-lumped and the second one is open-loop mode. To split these modes, we have to choose the resonator dimensions in such a way that the quasi-lumped resonance is located at the lower frequency band and the open-loop resonant mode is located at higher frequency band.

To be able to split the modes and to shift them to a lower frequency band, we have used a housing mount with width of 10 mm. That gives us more space to enlarge our resonator, which makes it easy to shift the modes. the other dimensions are kept the same as in Fig. [3.31.](#page-71-0)

Many dimensions affect the resonant frequencies of the filter. However, changing the outer dimensions of the resonator affects both mode resonances, which makes it difficult to fix one band on a certain frequency and tune the other. In order to do so,

there are two parameters that affect only one mode or one band. The first parameter is the width of the inductive transmission line  $(w)$ , which affects the quasi-lumped resonance, the wide the inductive strip is the lower the inductive value provided by this strip is, thus, the band is shifted to higher band by having wider strip line and vice versa. Fig. 6.10 shows the top and backside layouts of dual-band bandpass filter using splitted mode of dual mode suspended stripline resonator. The feeding lines are built on the topside of the substrate, while the resonators are constructed on the backside of the substrate. Fig. [6.11](#page-126-0) shows the insertion loss of the dual-band filter with different inductive stripline widths. As it is shown in the Figure, changing the width of the inductive strip line affects only the lower band without any effect on the higher one. The other parameter is the length of the open-loop resonator, which



Figure 6.10: Top (up) and backside of dual-bandpass filter using splitted mode of suspended stripline dual-mode resonator.

affects the open loop-mode. To avoid the influence of this parameter on the quasilumped resonance, the length of the open-loop resonator is shortened by increasing the width of the resonator  $(x)$  from the middle side and from the inner side, see Fig. 6.10. Fig. [6.12](#page-126-0) shows the insertion loss of the filter with different  $(x)$  values, as it is shown the upper band of the filter is moved to a higher frequency band by increasing the value of the dimension  $(x)$ .

With this configuration, a second order dual-band bandpass filter has been designed using this kind of resonators. The filter has center frequencies of 3.8 GHz and 8.85 GHz, with bandwidths of 200 MHz and 300 MHz, respectively. The length of the filter is 9.65 mm. Since the filter has been designed using two splitted-modes dual-mode resonators, each band of the filter can be considered second order bandpass filter. Fig. [6.13](#page-127-0) shows the simulated and measured insertion and return loss of the filter. The measured insertion loss at both passbands is better than 0.5 dB.

<span id="page-126-0"></span>

Figure 6.11: Insertion loss of the dual-band bandpass filter with deferent inductive stripline widths  $(w)$ .



Figure 6.12: Insertion loss of the dual-band bandpass filter with deferent  $x$  dimension values.

<span id="page-127-0"></span>

Figure 6.13: Simulated (dashed) and measured (solid) Insertion loss and return loss of the dual-band bandpass filter.

As it was shown in the same Figure, the stopband attenuation between the two passbands is about 23 dB, this rejection might not be sufficient for some application. Therefore transmission zeroes are needed between the passbands to improve the attenuation between the passbands. A transmission zero can be introduced there by applying additional inductive coupling between the resonators. This can be easily done by flipping one resonator by  $180^{\circ}$ , see Fig. [6.14.](#page-128-0) By this arrangement, the parallel inductive strips are now located on one side of the mount. A transmission zero is introduced at about 5.5 GHz. The measured and simulated return and insertion losses are shown in Fig. [6.15.](#page-128-0) An excellent agreement between the experimental and the theoretical results has been achieved.

<span id="page-128-0"></span>

Figure 6.14: Top (up) and backside (down) layouts of a suspended stripline filter with inductive stripline at one side of the substrate.



Figure 6.15: Simulated (dashed) and measured (solid) insertion and return loss of the dual-band bandpass filter with additional transmission zero.

# Chapter 7 Conclusions and Future Work

# 7.1 Thesis Summary

The thesis has discussed and introduced different filter and resonator types. Chapter three has investigated a modified cross-section of the multilayer coplanar line and applied it for filter applications. The advantages of this modified multilayer coplanar lines are the high capacitive coupling that it provides, furthermore it can easily integrated with CPW, microstrip line, or both. Compact filters have been introduced using this cross-section. Low-pass filter has been introduced using this cross section by adding wide patches to the classical CPW lowpass filter at the back side of the substrate and under the capacitive lines different compact filters have been introduced using this cross-section. Bandpass filters have been introduced using quasi-lumped elements, these filters have been constructed to be integrated with microstrip line, CPW, and both. Moreover, a suspended stripline UWB filter with a very wide stopband has been introduced by coupling lowpass filter capacitively with the I/O feeding lines.

In chapter four an interdigital DGS slot has been introduced. The slot is very compact compared to the other known slot structures, up to now. Controlling the resonant frequency of the slot is done by changing the metallic finger lengths, spacing between fingers, or by changing the number of the fingers. Two lowpass filters have been presented using this slot showing the advantage of the compact slot. Moreover, the chapter has discussed the packaging difficulties of this technique and presented a solution to reduce the packaging difficulties by keeping the ground plane of the circuit fully metallized and etching the slots on the superstrate, which is directly lain on the top of the substrate. The metal of the superstrate is connected by via holes to the ground plane. The structure has the great advantage in reducing the packaging complexity, since it can be directly based on the carrier block without the need of machining a recessed region in it.

Chapter five introduced the first microstrip realization of triple-mode resonator.

This resonator was realized by adding an additional meander half wavelength microstrip line connected to two opposite corners of the original microstrip square-loop dual-mode resonator. The resonator was coupled capacitively by two perpendicular feeding lines. The position of the transmission zeros depends on the connection positions of the feeding lines. In the centered case, the filter shows one attenuation pole and two complex transmission zeros. By introducing a non-symmetry into the positions of the feeding lines, the transmission zeros are moved on to the imaginary axis of the s-plane. Equivalent circuit and coupling scheme has been presented. Two different third-order band pass filters were designed, fabricated, and measured. Good agreement has been obtained between the measured and theoretical results. In the same chapter, a realization suspended stripline dual-mode resonator has been introduced, which is the first dual-mode resonator for this technique. The resonator was realized by combining quasi-lumped parallel resonator with open-loop resonator. The resonator was applied to filter design. Very compact bandpass filters have been designed fabricated and tested. Transmission zeroes have been introduced to the filter response by applying additional inductive coupling between the resonators.

In chapter six dual-band bandpass filters have been realized by using dual-mode resonators. The first filter is a microstrip one, it has been realized by introducing transmission zeros in the passband of a broadband bandpass filter by using squareloop dual-mode resonator. controlling the center frequencies of both bands can be done by changing the length of the attached transmission lines and the length of the arms of the loop resonator equally. Controlling the bandwidth of both bands can also be done by either by changing the length of the attached transmission lines and fixing the length of the arms loop resonator, or by changing the length of the arms of the loop resonator and keeping the attached transmission line lengths fixed. The second introduced filter in this chapter was a suspended stripline one. the filter was realized by splitting the modes of the dual-mode resonator that is introduced in the last chapter into two frequency bands. transmission zero has been introduced between the two frequency bands by applying additional inductive coupling between the reosnotors.The dual-mode resonator has shown that it is an excellent resonator for filter applications especially for dual-band bandpass filter application.

## 7.2 Suggestions for Future Work

This thesis has presented and investigated different filter topologies and responses for different planar techniques. Since the development of the communication systems is increasing rapidly, and since the filters are essential component in any communication system, the author would like to suggest some ideas for future work.

1. For the DGS structure, it is an important issue to investigate broadband filters using this technique. Moreover, the thesis have introduced a packaging solution for the DGS, it might be also important to introduce and investigate other packaging solutions.

- 2. Quadra-mode bandpass resonator may be realized by adding an additional path to the triple-mode resonator, which can decrease the size of the filter, and may increase the number of transmission zeros introduced in the stopband of the filter. For the suspended stripline, more investigation is needed on the triplemode resonators.
- 3. In the dual-band bandpass filters, it might be interesting to introduce and investigate new tunable dual-band filters. Moreover, it might also be interesting to investigate a quadrable band diplexers using two dual-bandbandpass filters.

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# Curriculum Vitae



#### Education

- Since 06.2005: Working towards Ph.D. degree at the Institute for Electronics, Signal Processing, and Comm., University of Magdeburg, Germany.
- 04.2002 02.2005: M.Sc. in Communication Technology, University of Ulm, Ulm, Germany.
- 10.1996 06.2000: B.Sc. in Physics / Minor Electronics, An-najah National University, Nablus, Palestine.

### Work Experience

- 01.2004 03.2005: Testing and integrating mobile phone software on various platforms, LogicaCMG Ulm, Ulm, Germany.
- 02.2003 08.2003: Thermal analysis with differential scanning calorimeter (DSC) Dept. of Advanced Materials, University of Ulm, Ulm, Germany.
- 02.2003 08.2003: Assistant lecturers for maths and physics Der Sharaf Secondary School, Nablus, Palestine.

### Memberships

- Editorial Board Member of IEEE Microwave and Wireless Components Letters.
- Editorial Board Member of Journal of Electromagnetic Waves and Applications.

## List of Publications

#### Journal Papers:

- 1. Atallah Balalem, Jan Machac, and Abbas Omar, ["Dual-Band Bandpass](http://www3.interscience.wiley.com/cgi-bin/fulltext/117948798/PDFSTART) [Filter Using the Microstrip Square-Loop Dual-Mode Resonator"](http://www3.interscience.wiley.com/cgi-bin/fulltext/117948798/PDFSTART), Microwave and Optical Technology Letters, Vol. 50, No. 6, pp. 1567-1570, June 2008.
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- 6. Wolfgang Menzel, Atallah Balalem, ["Quasi-Lumped Suspended Stripline](http://ieeexplore.ieee.org/stamp/stamp.jsp?arnumber=1516329&isnumber=32483) [Filters and Diplexers"](http://ieeexplore.ieee.org/stamp/stamp.jsp?arnumber=1516329&isnumber=32483), IEEE Transactions on Microwave Theory and Techniques , Vol. 53, No. 10, pp. 3230-3237, October 2005. (cited 9 times)

#### Conference Papers:

- 7. Adel Abdel-Rahmand, Atallah Balalem, Jan Machac, and Abbas Omar, "UWB Bandpass Filter with Wide Stopband Using Lumped Coupling Capacitors", Asian Pacific Microwave Conf. 2009 (APMC 2009), Singapore, December 2009.
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