

# Novel Sound Imaging Method for the Localization of Leakages in Machines and Drives based on Moving Microphones

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## Abstract

This contribution describes a novel method for visualizing acoustic leakages in machines, drives and generic mechanical structures using a rotating linear array of a few digital ultrasound microphones in combination with a multi-frequency ultrasound transmitter. The rotating array scans the incident sound field generated by the ultrasound transmitter on a circular area. In a typical measurement setup, the ultrasound transmitter is placed in a cavity (e.g. machine housing, gearbox case) and operates at distinct harmonic frequencies at around 40kHz in an omnidirectional fashion. The rotating linear array is operated on the outside of the cavity and captures the sound field escaping through small leakages. While the reduced hardware complexity allows for the design of a lightweight, handheld sound imaging device, the algorithmic portion of the measurement system requires special attention. In fact, established methods of sound imaging like beamforming and nearfield holography cannot be applied to signals stemming from moving sensors. The proposed method of computing an acoustic image using the described measurement setup is based on compensating the moving microphone signals for Doppler distortions and evaluating the coherence of the resulting signals with a non-moving reference microphone for each point in the acoustic image. The setup and methodology is evaluated for leakage and tightness testing of machinery components and structures in a quality control context. The corresponding troubleshooting process from assessment and quantification of the situation to resolution of the root cause is described from a user perspective.

## Kurzfassung

Dieser Beitrag beschreibt eine neuartige Methode zur Visualisierung von akustischen Leckagen in Maschinen, Antrieben und allgemeinen mechanischen Strukturen mithilfe eines rotierenden linearen Arrays mit digitalen Ultraschallmikrofonen in Kombination mit einem Ultraschallsender. Das rotierende Array scannt das von dem Ultraschallsender erzeugte einfallende Schallfeld auf einem kreisförmigen Bereich. In einer typischen Messanordnung wird der Ultraschallsender in einem Hohlraum (z.B. Maschinengehäuse, Getriebegehäuse) platziert und erzeugt ein homogenes Schallfeld bei 40 kHz. Das rotierende lineare Array wird außerhalb des Hohlraums betrieben und erfasst den durch kleine Leckagen entweichenden Schall. Während die reduzierte Hardwarekomplexität die Entwicklung einer leichten, handgehaltenen akustischen Kamera ermöglicht, erfordert der algorithmische Teil des Messsystems besondere Aufmerksamkeit. Tatsächlich können etablierte Methoden der Schallbildgebung wie Beamforming und Nahfeld-Holographie nicht auf Signale angewendet werden, die von bewegten Mikrofonen erzeugt werden. Die vorgeschlagene Methode zur Berechnung eines akustischen Bildes unter Verwendung der beschriebenen Messanordnung basiert auf der

Kompensation der Doppler-Verzerrungen der sich bewegenden Mikrofon-signale und der Auswertung der Kohärenz der resultierenden Signale mit einem unbeweglichen Referenzmikrofon für jeden Punkt im akustischen Bild. Die Einrichtung und Methodik wird für Leckage- und Dichtheitstests von Maschinenkomponenten und -strukturen im Kontext der Qualitätskontrolle evaluiert. Der entsprechende Fehlerbehebungsprozess von der Bewertung und Quantifizierung der Situation bis zur Behebung der Ursache wird aus Benutzersicht beschrieben.

## 1. Introduction

This paper addresses the topic of leakage visualization in machines and drives based on a transmitter-receiver setup where the transmitter is a speaker operating in the ultrasound domain and the receiver is a measurement instrument comprising a multitude of ultrasound microphones.

An overview of existing technologies using such a transmitter-receiver setup is given in section “State of the Art” where the foundation for motivating a receiver design based on a rotating linear microphone array is laid.

In section “Sensor Concept”, the authors describe the hardware related properties of the sensor and the special characteristics of acoustic data captured with the proposed sensor.

Section “Acoustic Image Computation” explains in detail how the acoustic signals captured by the sensor are processed to generate heatmaps showing the spatial position and strength of leakages.

In section “Applications”, actual measurement results from machine enclosures are depicted and analyzed.

## 2. State of the Art

The ultrasound microphone is a widely accepted sensor device for detecting leakages in industrial infrastructure, e.g. compressed air lines, gas pipelines, pressure vessels. A crack, fissure or porosity in the structure causes the gas to escape and produces a stationary bandlimited sound in the ultrasound frequency domain. The acoustical footprint of the leakage depends on parameters such as defect geometry, pressure differential and gas type but early indications of a leakage can be typically detected in the range of 30-40kHz [1]. To enable humans to search for a leakage, the captured acoustical signal is downconverted to the audible frequency band. When the microphone gets closer to the leakage, the perceived loudness of the downconverted hissing sound increases

When performing leakage detection for machines and drives such as a door, window, trunk or bulkhead, the sound escaping through seals, gaskets, grommets and other imperfections has to be generated. For doing so, an ultrasound transmitter is put inside the cavity or cabin of interest. This device typically comprises a multitude of loudspeakers emitting sound in an omnidirectional fashion at multiple distinct frequencies at about 40kHz, thus creating a homogenous sound pressure field at the positions where leakages shall be checked.

Instead of logging the corresponding sound pressure levels along the paths of interest, it is common practice to rely on cues from loudness variations in the downconverted acoustical signal when searching for dominant leakages. Since the loudness may only vary within a certain dynamic range, it is required to first dial in on an expected loudness level. Having to focus on loudness variations over a longer period of time may lead to fatigue and lack of concentration.

Ultrasound imaging has, thus, become an attractive alternative to surface bound probing with an ultrasound microphone because visualizing leakages from a distance allows capturing a larger area at once, gives consistent quantification across that area and does not distort the sound pressure field caused by the presence of the measurement device.

Ultrasound imaging devices are typically implemented as two-dimensional microphone arrays with up to about 130 ultrasound microphones distributed over a circular area with a diameter of less than 15cm and a camera to overlay the acoustical heatmap and the optical image of the measurement scene. The imaging performance of ultrasound imaging devices is mostly governed by two contributors, namely the diameter of the microphone array and the number of microphones distributed over that area. The array diameter predominantly sets the spatial resolution. The larger the array diameter, the higher the spatial resolution is, see section "Sensor Concept" for a detailed explanation. The number of microphones influences the dynamic range of the resulting acoustic image, i.e. the maximum difference in loudness level that can be resolved. Also, a higher count of distributed microphones directly translates into a lower minimum detectable sound pressure level due to an improved signal-to-noise ratio.

Since ultrasound leakages in machinery applications are typically measured at a distance of 0.75 to 1.5 meters, the signal-to-noise ratio and, thus, the number of microphones becomes essential. Also, spatial resolution at the excited frequency of the ultrasound transmitter is essential, see section "Sensor Concept" for a detailed explanation.

While ultrasound imaging devices enable a fast measurement and analysis, it shall still be noted that – at the time of this publication - the weight of available handheld devices is close to or above the recommended maximum weight of 2.3kg for handheld equipment per standard MIL-HDBK-759C [2]. Using such equipment for an extended period of time may pose the risk of tiring of the hand-arm-system.

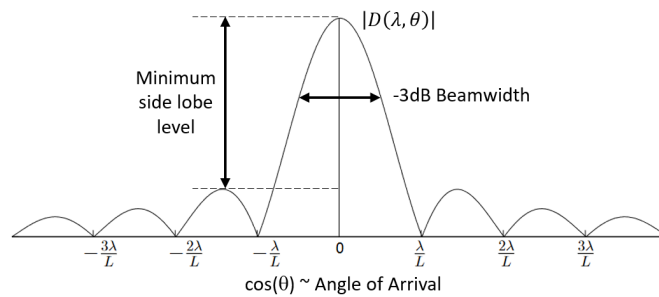
These performance and ergonomics criteria have led the authors to propose a new sensor concept targeting at high spatial resolution and dynamic range, low minimum detectable sound pressure level and comfortable use.

### 3. Sensor Concept

The proposed sensor concept is motivated by the underlying physics describing the spatial resolution and dynamic range of a sound imaging system. For simplicity, we consider a sensor with a linear, continuously distributed sensing capability with aperture length  $L$ . The corresponding normalized, horizontal directivity pattern  $D$  is given by

$$D(\lambda, \theta) = \text{sinc} \left( \frac{L}{\lambda} \cos \theta \right) \quad (1)$$

where  $\theta$  is the angle of arrival of an incident sound wave and  $\lambda = c/f$  is the wavelength,  $c$  is the speed of sound in air and  $f$  is the sound frequency [4] [5] [6]. The shape of the directivity function is depicted in Figure 1. In this configuration, the distributed sensor is most sensitive for sound waves coming in at zero degree and its sensitivity degrades for waves approaching at other angles.



**Figure 1:** Normalized, horizontal directivity pattern  $D$  for a continuous linear array with aperture length  $L$  evaluated at wavelength  $\lambda$

The spatial resolution of a sound imaging system is typically quantified by the  $-3\text{dB}$  beamwidth of the main lobe. An improved spatial resolution can therefore be achieved in two ways: (i) increasing the aperture length  $L$  or (ii) increasing the frequency of the sound event. Option (i) essentially translates into an increased size of the sensor which, as we will see later on, requires a higher count of distributed microphones and, thus, impacts the hardware complexity. Option (ii) may potentially be an available parameter in applications where the excitation frequency of the ultrasound transmitter can be controlled. Yet, it shall be considered that the higher the excitation frequency is, the more difficult it becomes to implement an ultrasound transmitter with both omnidirectional characteristics and sufficient sound power.

The side lobes in Figure 1 play a special role for real arrays with a finite number of discrete microphones. In fact, the side lobe level quantifies the dynamic range of a sound imaging system. If, for instance, the side lobe level at a certain frequency is  $10\text{dB}$  below the main lobe level and assuming that all involved sound sources can be spatially resolved, then the imaging system is still able to localize secondary sources with a pressure level less than  $10\text{dB}$  below the most dominant source. The dynamic range can be improved by increasing the number of distributed microphones which, again, impacts the hardware complexity.

In order to get a better impression of the actual numbers that the above formulae suggest, we consider two leaks having a distance between each other in the range of

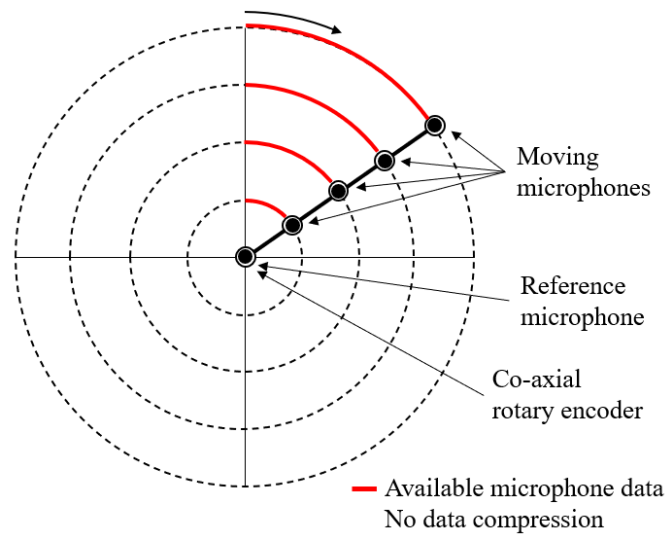
about  $d_1 = 10\text{cm}$ . Resolving leakages measured at a distance of about  $d_2 = 75\text{cm}$  ideally requires the main lobe to have an opening angle of less than  $\theta_{max} = \left(\frac{d_1/2}{d_2}\right) = 0.13\text{rad} = 7.63^\circ$ . When detecting leakages at 40kHz in air, this translates into a minimum array diameter of  $L_{min} = \lambda/\sin \sin(\theta_{max}) = 4.1\text{cm}$  with  $\lambda = 343\text{ms}^{-1}/40.000\text{Hz}$ , see Figure 1 and equation (1).

Considering the typical landing pattern of a digital MEMS microphone which is in the range of 4mm by 6mm, the hardware implementation of an array with a high count of microphones for optimum dynamic range can easily become a realization problem.

Based on these insights and trade-offs, the authors propose a sensor concept which enables high spatial resolution and high dynamic range while targeting minimum array size, weight and complexity of the associated sensor hardware.

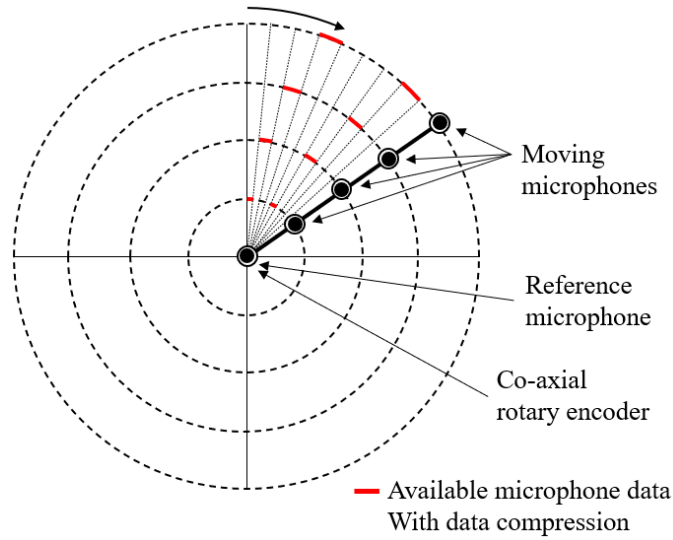
### 3.1 Hardware implementation

The centerpiece of the sensor concept is a rotating linear array with five distributed microphones which pivots about a non-moving reference microphone. The trajectory of the remaining moving microphones is described by concentric circles. A magnetic rotary encoder which is co-axially aligned with the rotation axis of the array, measures the angular position with respect to the spatially constrained axis of rotation, see Figure 2.



**Figure 2:** Rotating linear array comprising five microphones pivoting about the reference microphone. The trajectory of the moving microphones is described by concentric circles

The microphones are based on digital MEMS technology and the corresponding signals are acquired over a common signal path using the time division multiplexing (TDM) method. This method enables the straightforward implementation of a microphone multiplexing scheme for data compression and emulation of arbitrary, even non-implementable two-dimensional array geometries. For instance, the data acquisition can be configured such that the reference microphone along with a second channel which periodically switches between the moving microphones, are recorded, see Figure 3.



**Figure 3:** Multiplexing of the moving microphones enables data compression and emulation of arbitrary two-dimensional array geometries

It is well known that the directivity pattern of the array and the corresponding position of microphones can be optimized to meet certain performance criteria, e.g. the minimum side lobe level at specific frequencies. While two-dimensional arrays with discrete microphone positions require a complete hardware reconfiguration in terms of repositioning the microphones, the rotating linear array merely requires a software reconfiguration to acquire the data at different positions.

Also, the implementation of large arrays with a diameter of more than one meter does not increase the hardware complexity. In fact, the number of microphones distributed along the linear array can stay the same since the fine spatial sampling along the concentric circles guarantees adherence to the spatial sampling theorem [3] [4].

The rotating linear array is a self-powered system and uses wireless technology for data transmission of the audio and rotary encoder data to a processing unit.

### 3.2 Properties of signals acquired by moving microphones

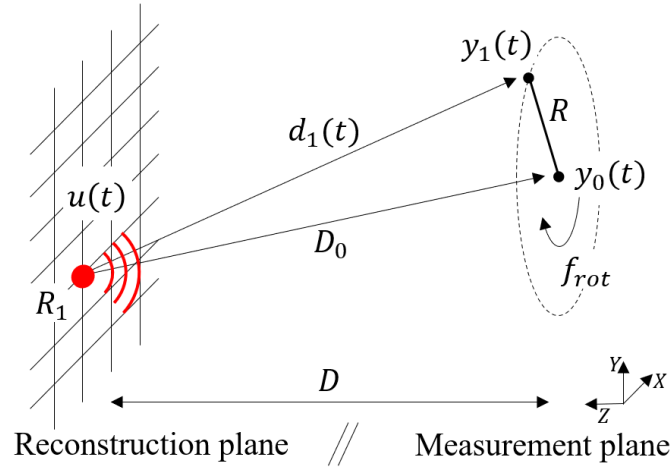
In order to better understand the characteristics of a signal acquired by a moving microphone, we consider a point source with harmonic excitation signal  $u(t)$  at the frequency  $f_0$

$$u(t) = \text{Re}\{e^{i2\pi f_0 t}\}. \quad (2)$$

Assuming that the corresponding sound wave is independent from the distance to the source and the rotational speed  $f_{rot}$  of the moving microphone is constant, the audio signal  $y_1(t)$  captured by the moving microphone is given by

$$y_1(t) = \text{Re}\left\{e^{i2\pi f_0 t} e^{-i2\pi f_0 \frac{d_1(t)}{c}}\right\} \quad (3)$$

where  $d_1(t)$  is the time-varying distance between the sound source and the position of the moving microphone along its circular trajectory with radius  $R$ , see Figure 4.



**Figure 4:** Notations used for describing the setup comprising a point source in the reconstruction plane and a reference microphone and a moving microphone located in the measurement plane

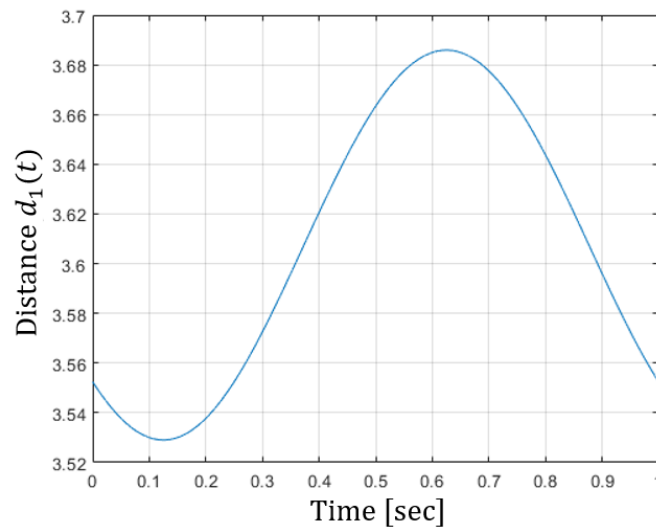
We further denote the constant distance between the sound source at reconstruction point  $R_1$  and the stationary reference microphone by  $D_0$ , the corresponding audio signal by  $y_0(t)$

$$y_0(t) = \text{Re} \left\{ e^{i2\pi f_0 t} e^{-i2\pi f_0 \frac{D_0}{c}} \right\} \quad (4)$$

and the distance between the parallel reconstruction and measurement planes by  $D$ . The origin of the Cartesian coordinate system with point representation given by  $(X, Y, Z)$  is at the position of the reference microphone and the  $XY$ -plane is the measurement plane. Considering the parameters

$$f_0 = 1\text{kHz}, f_{rot} = 1\text{Hz}, R = 1\text{m}, D = 3\text{m}, D_0 = (-0.1\text{m}, -0.1\text{m}, D), \quad (5)$$

we get the following result for the time-varying distance  $d_1(t)$  and the short-time Fourier transformation of the audio signal  $y_1(t)$ , see Figure 5 and Figure 6.



**Figure 5:** The time-varying distance between the sound source and the position of the moving microphone along its circular trajectory.

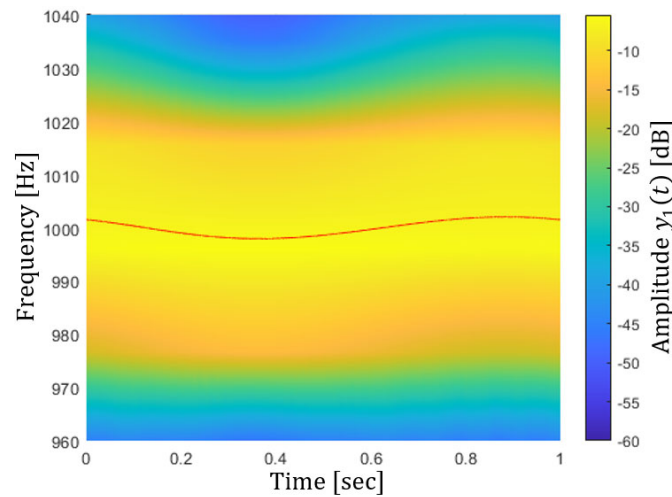
As expected, the short-time Fourier transformation of the moving microphone signal  $y_1(t)$  is a Doppler-shifted version of the original source signal  $u(t)$ .

## 4. Acoustic Image Computation

The measurement setup depicted in Figure 4 along with the basic observations on the signal properties of the moving microphone and reference microphone signals now enable us to derive an algorithm for the computation of a map describing the distribution of sound sources in the reconstruction plane.

### 4.1 The case of perfect Doppler shift compensation

As a first step, we map the signal  $y_1(t)$  of the moving microphone to the spatial position of the reference microphone. This transformation involves backpropagating  $y_1(t)$  to the point of the sound source in the reconstruction plane using the time-varying distance  $d_1(t)$  and then forward propagating the signal to the reference microphone position using the constant distance  $D_0$ .



**Figure 6:** The short-time Fourier transformation of the moving microphone signal for the time-varying distance  $d_1(t)$  depicted in Figure 5.

The resulting signal  $\underline{y}_1(t)$

$$\underline{y}_1(t) = y_1(t + d_1(t) - D_0) = \text{Re} \left\{ e^{i2\pi f_0 t} e^{-i2\pi f_0 \frac{(d_1(t) - d_1(t) + D_0)}{c}} \right\} = y_0(t) \quad (6)$$

has the obvious property that the Doppler shift previously induced in  $y_1(t)$  is fully compensated and is identical to the signal captured at the position of the reference microphone.

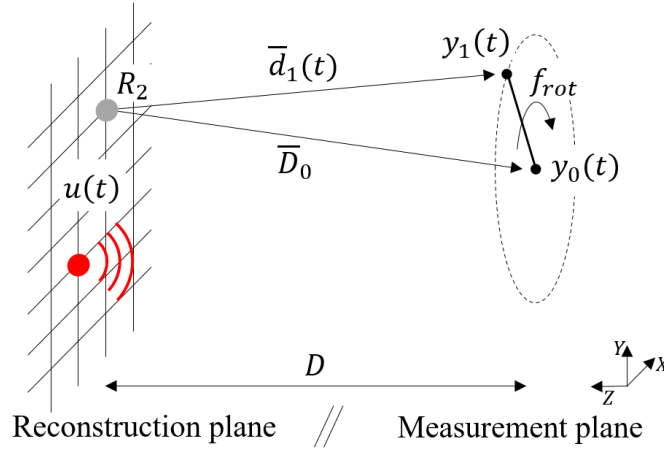


## 4.2 The general case

We now consider the transformation for a point  $R_2$  in the reconstruction plane which is at a constant distance  $\underline{D}_0$  from the reference microphone position and away from the point source, see Figure 7.

An additional Doppler shift is induced in the transformed signal  $\underline{y}_1(t)$  given by

$$\underline{y}_1(t) = y_1(t + \underline{d}_1(t) - \underline{D}_0) = \text{Re} \left\{ e^{i2\pi f_0 t} e^{-i2\pi f_0 \frac{(d_1(t) - \underline{d}_1(t) + \underline{D}_0)}{c}} \right\}. \quad (7)$$



**Figure 7:** Notations used for describing the setup when mapping the moving microphone signal  $y_1(t)$  to the reference microphone position via the point  $R_2$  in the reconstruction plane.

Now, we apply the coherence function  $C_{\underline{y}_1 y_0}(f)$  as a frequency-dependent measure of statistical similarity of the transformed signal  $\underline{y}_1(t)$  and the signal  $y_0(t)$  captured the reference microphone position,

$$C_{\underline{y}_1 y_0}(f) = \frac{|S_{\underline{y}_1 y_0}(f)|^2}{S_{\underline{y}_1 \underline{y}_1}(f) S_{y_0 y_0}(f)} \quad (8)$$

where  $S_{\underline{y}_1 y_0}(f)$  is the cross-spectral density of the signals  $\underline{y}_1(t)$  and  $y_0(t)$  and  $S_{\underline{y}_1 \underline{y}_1}(f)$  and  $S_{y_0 y_0}(f)$  are the power spectral density functions of  $\underline{y}_1(t)$  and  $y_0(t)$ , respectively [6]. The coherence function varies in the interval  $0 \leq C_{\underline{y}_1 y_0}(f) \leq 1$ . We get a high coherence value at a specific frequency  $f$  for points in the reconstruction plane where a sound source is actually located, and a low coherence value for points where there is no or little sound radiation.

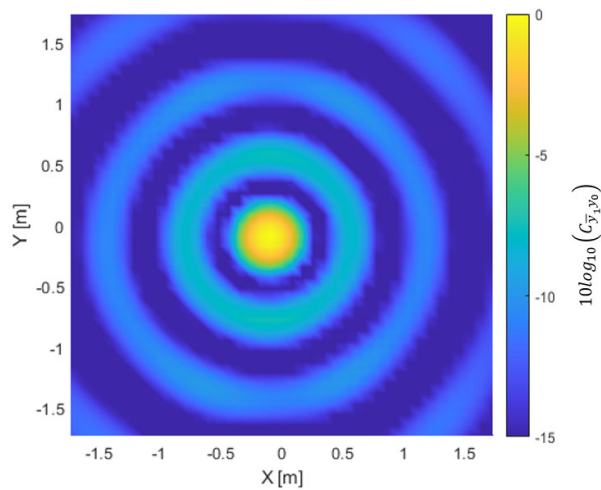
We can now use this metric to produce a heatmap representing the distribution of sound sources over the entire reconstruction plane. Considering the parameters from Equation (5) and a point source at the spatial position  $(-0.1m, -0.1m, -D)$ , we get the color-coded representation of the coherence function  $C_{\underline{y}_1 y_0}(f)$  evaluated at  $f = 1kHz$  depicted in Figure 8. With this special set of parameters, the resulting heatmap is also

referred to as point spread function (PSF) which is used to quantify the performance of an imaging system in terms of spatial resolution and dynamic range [3].

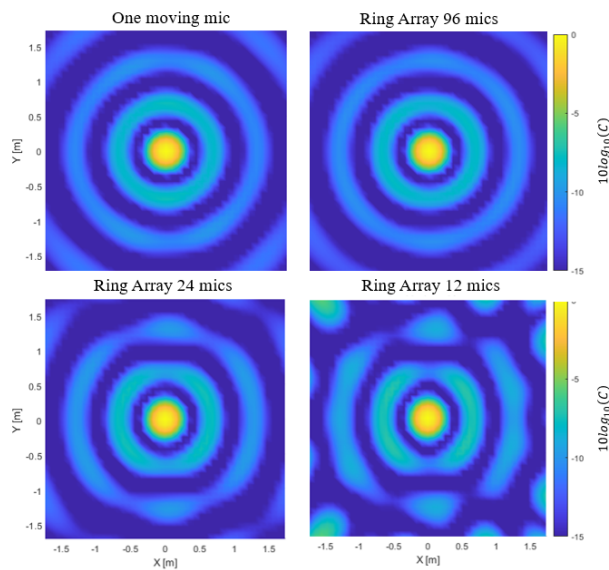
### 4.3 Comparison with fixed arrangement of microphones

In order to appreciate the image quality achieved with one moving microphone only, we can compute the coherence function for a hardware setup with a fixed spatial arrangement of microphones equally spaced along the trajectory of the moving microphone. Figure 9 depicts the result for 12, 24 and 96 microphones.

It is readily visible that the coherence function for the arrangement of 96 microphones approaches the result from the moving microphone. Using 12 microphones only leads to the well-known artifact of grating lobes caused by spatially undersampling the incident sound field [4].



**Figure 8:** Logarithmic representation of the coherence function  $C_{y_1, y_0}(f)$  evaluated at  $f = 1\text{kHz}$ .

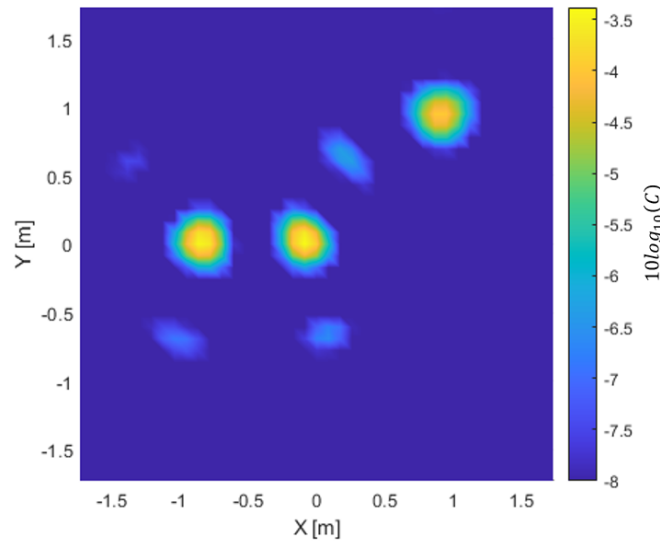


**Figure 9:** Coherence function  $C_{y_1, y_0}(f)$  for fixed spatial arrangement of 12m, 24 and 96 microphones evaluated versus one moving microphone.

## 4.4 Multiple distributed sound sources

Before we evaluate the capabilities of the proposed sensor concept in real world applications, we finish this section by computing the distribution of multiple sound sources of equal strength emitting a tone at 1kHz and located at positions  $P_1 = (-1m, 0, D)$ ,  $P_2 = (0, 0, D)$ ,  $P_3 = (1m, 1m, D)$  in the reconstruction plane, see Figure 10.

We shall note that the artifacts surrounding the three sound sources are coming from the mutual, positive interference of the point spread functions at the three spatial positions, thus, degrading the useable dynamic range.



**Figure 10:** Coherence function  $C_{y_1 y_0}(f)$  for multiple sound sources emitting a tone at 1kHz and located at positions  $P_1 = (-1m, 0, D)$ ,  $P_2 = (0, 0, D)$ ,  $P_3 = (1m, 1m, D)$  in the reconstruction plane.

## 5. Applications

The proposed sensor concept is now applied to leakage and tightness testing of a machine enclosure of a medical device in a quality control context.

### 5.1 Measurement setup

The measurement setup comprises the following devices:

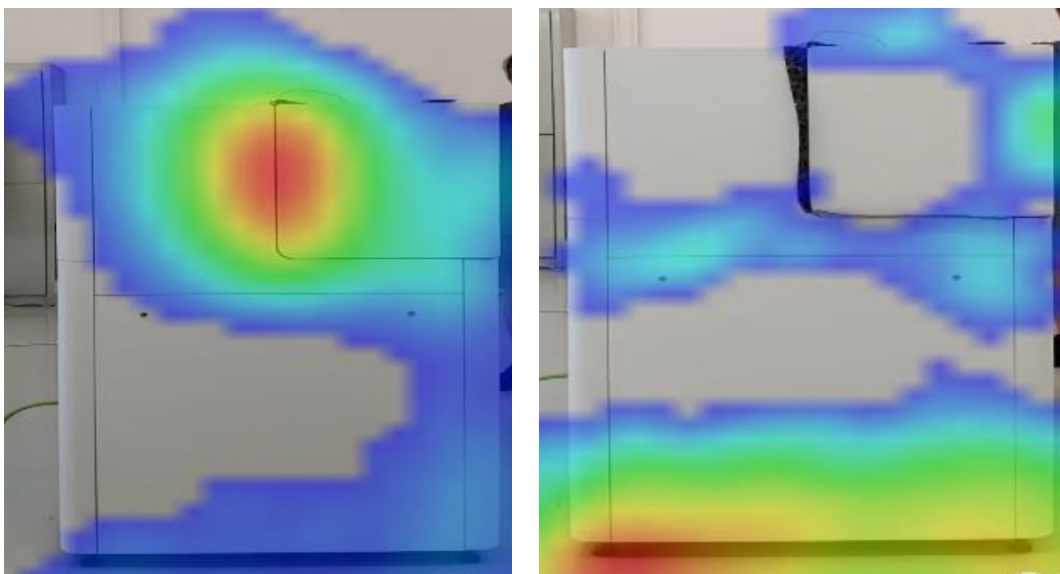
- a rotating sensor with a total of eight microphones sampled at 130kHz and equally distributed over a length of 6cm with one reference microphone at the center of rotation and seven microphones moving along circular trajectories on a disc with a maximum diameter of 12cm,
- an omnidirectional ultrasound loudspeaker (manufacturer: SDT, model: T-Sonic9) placed inside the machine enclosure and generating ultrasound at 39,9kHz and 40,1kHz at a stable sound pressure level of 113dB measured at a distance of 1m under free field conditions,

- a mobile device (model: Samsung A71) for capturing the audio as well as rotary encoder data and sending the data to
- a high-performance laptop (model: Dell precision 7550) for computing the acoustic images.

The sensor is positioned at a distance of 2m away from the device. The sensor rotates at a speed of two revolutions per second producing twelve acoustic images per second. The incident sound field is spatially sampled by the moving multiplexed microphone at 180 sectors per revolution, also see Figure 3. The optical image is taken with a horizontal field of view of 69,5°.

## 5.2 Measurement process

For the measurement scenario depicted in Figure 11 on the left, we see a dominant leak at the vertical gap at 64,5dB with a dynamic range of 8dB. When applying additional insulation material, the sound pressure level drops by 6dB and the dominant sound emissions come from underneath the device which is considered to be the nominal footprint.



**Figure 11:** Leakage at the vertical gap between the lid and the enclosure at 64,5dB with a dynamic range of 8dB (left). When applying additional insulation material to the lid, the maximum sound pressure level of the acoustic image is reduced to 58,8dB (right).

As part of a rigorous, data based quality control scheme, each device can be tested end of line and assessed in terms of pass-fail criteria with respect to tightness of critical structures. Reasonable criteria can be the maximum allowable sound pressure level in a certain region of interest or quantified deviations from an expected distribution of leakages with associated pressure levels. Any deviation with respect to these criteria can be an indication of a faulty assembly and, thus, lead to excessive noise emissions from inside the machine and violation of regulatory noise limits.

## 6. Summary/Conclusions

This contribution addressed the topic of leakage visualization in machinery structures based on a new sensor concept which involves a rotating sensor with multiple ultrasound microphones scanning a circular area. The underlying measurement method is derived and its performance properties are described. A measurement setup comprising the above mentioned sensor, an ultrasound transmitter, a mobile device and high-performance laptop is used to produce acoustic images for quality control in a quality control context.

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